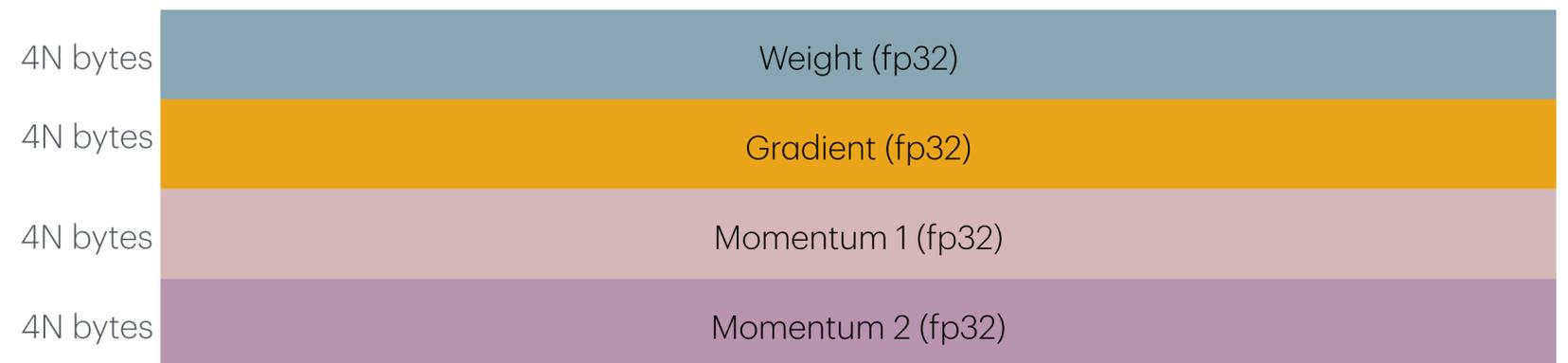


# Low-rank adapters

# Training large models

## Memory requirements

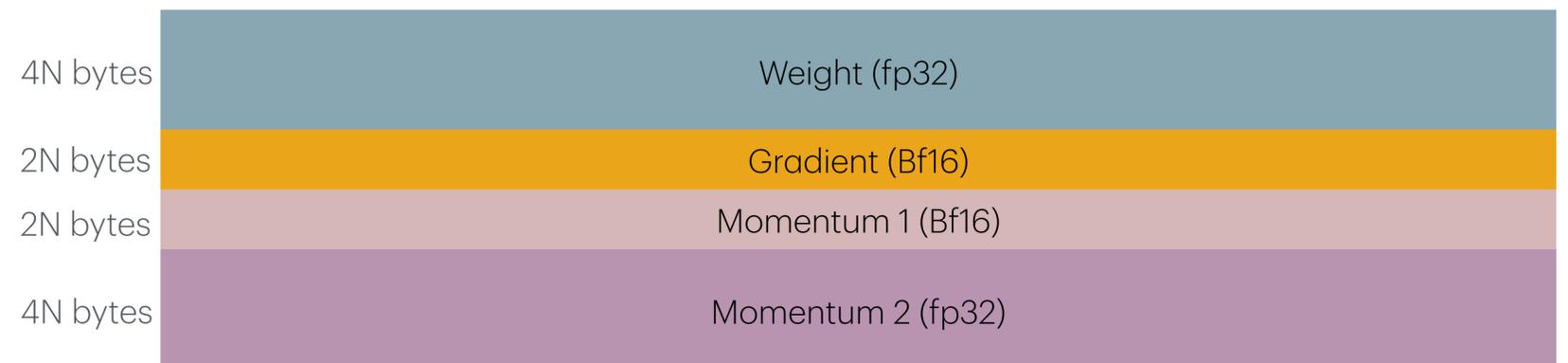
- Without optimization:
  - Model parameters:  $N$
  - Weights:  $N$  floats
  - Gradients:  $N$  floats
  - Momentum:  $N$  floats
  - 2nd momentum (ADAM):  $N$  floats
- $16N$  bytes without counting activations



# Training large models

## Memory requirements

- Mixed precision
  - Model parameters:  $N$
  - Weights:  $N$  floats
  - Gradients:  $N$  bfloat16
  - Momentum:  $N$  bfloat16
  - 2nd momentum (ADAM):  $N$  floats
- $12N$  bytes without counting activations



# Training large models

## Memory requirements

- Zero / FSDP
- $16N / M$  bytes without counting activations
- For  $M$  GPUs
  - Good solution for GPU-rich people

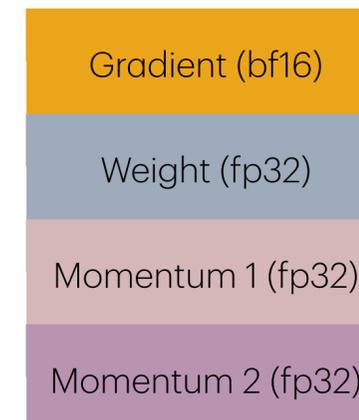
4N bytes

4N bytes

4N bytes

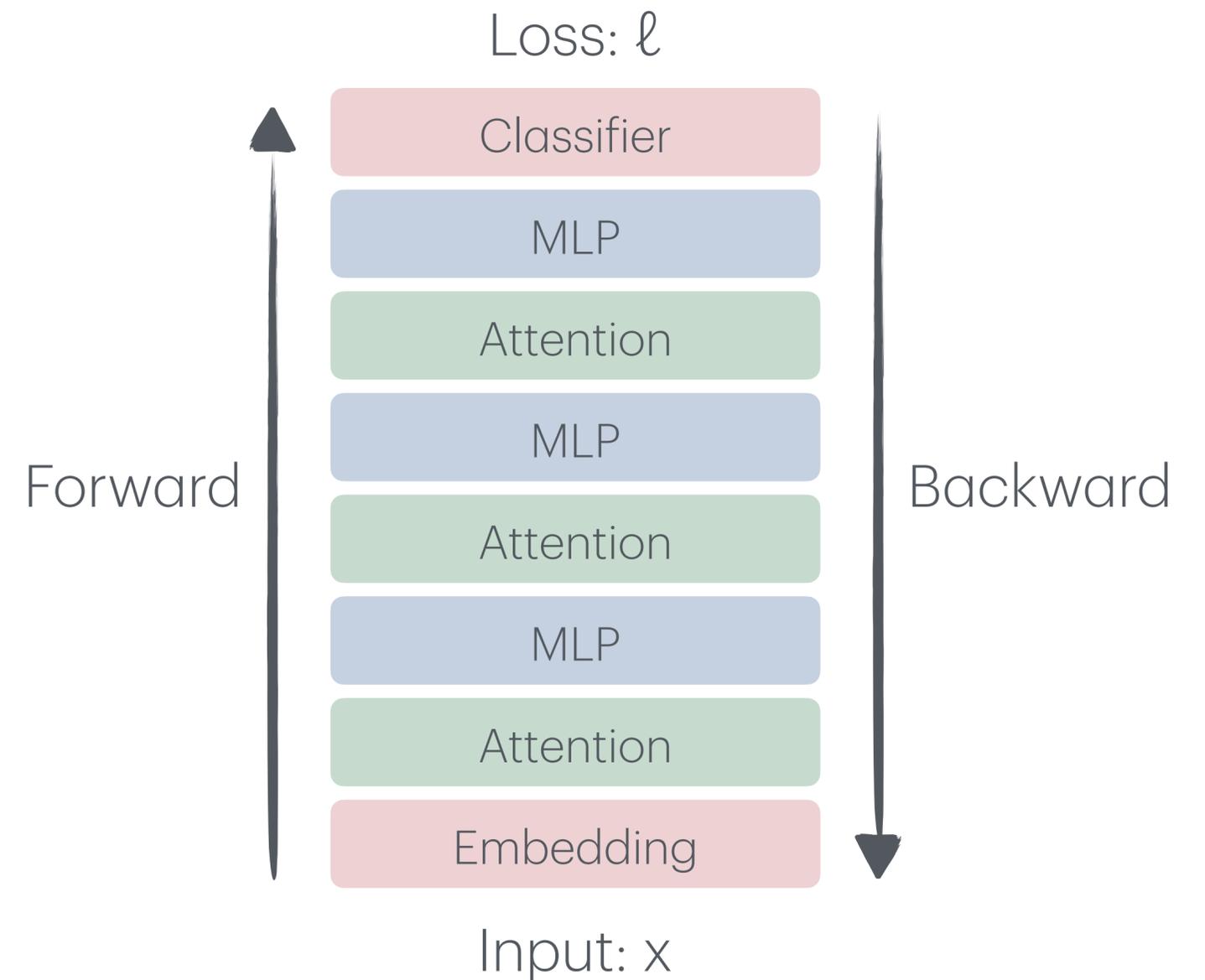
4N bytes

FSDP



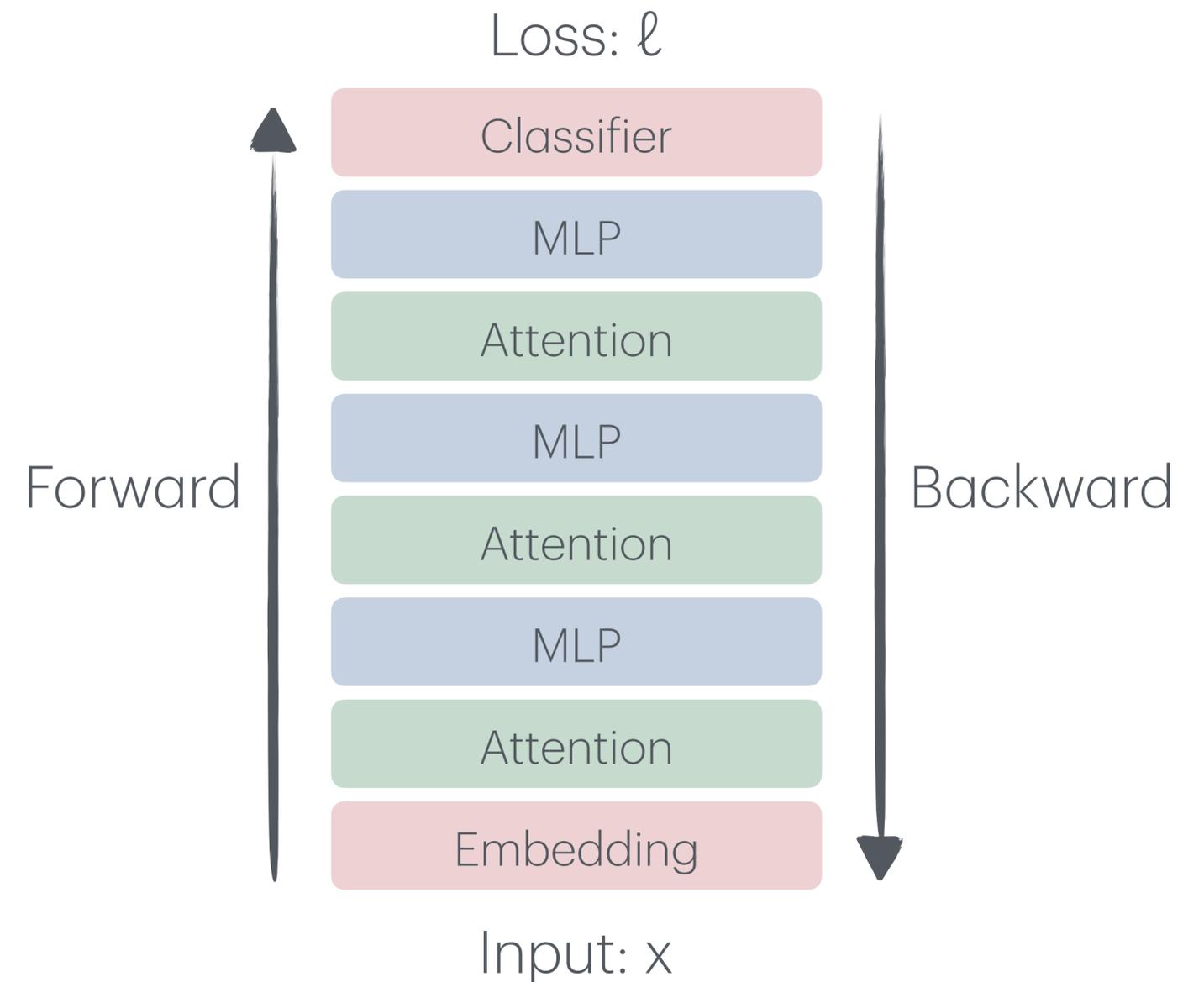
# Memory Use

- What takes up GPU memory during training?
  - Model weights
  - Gradients
  - Momentum
  - Activations (more later in class)



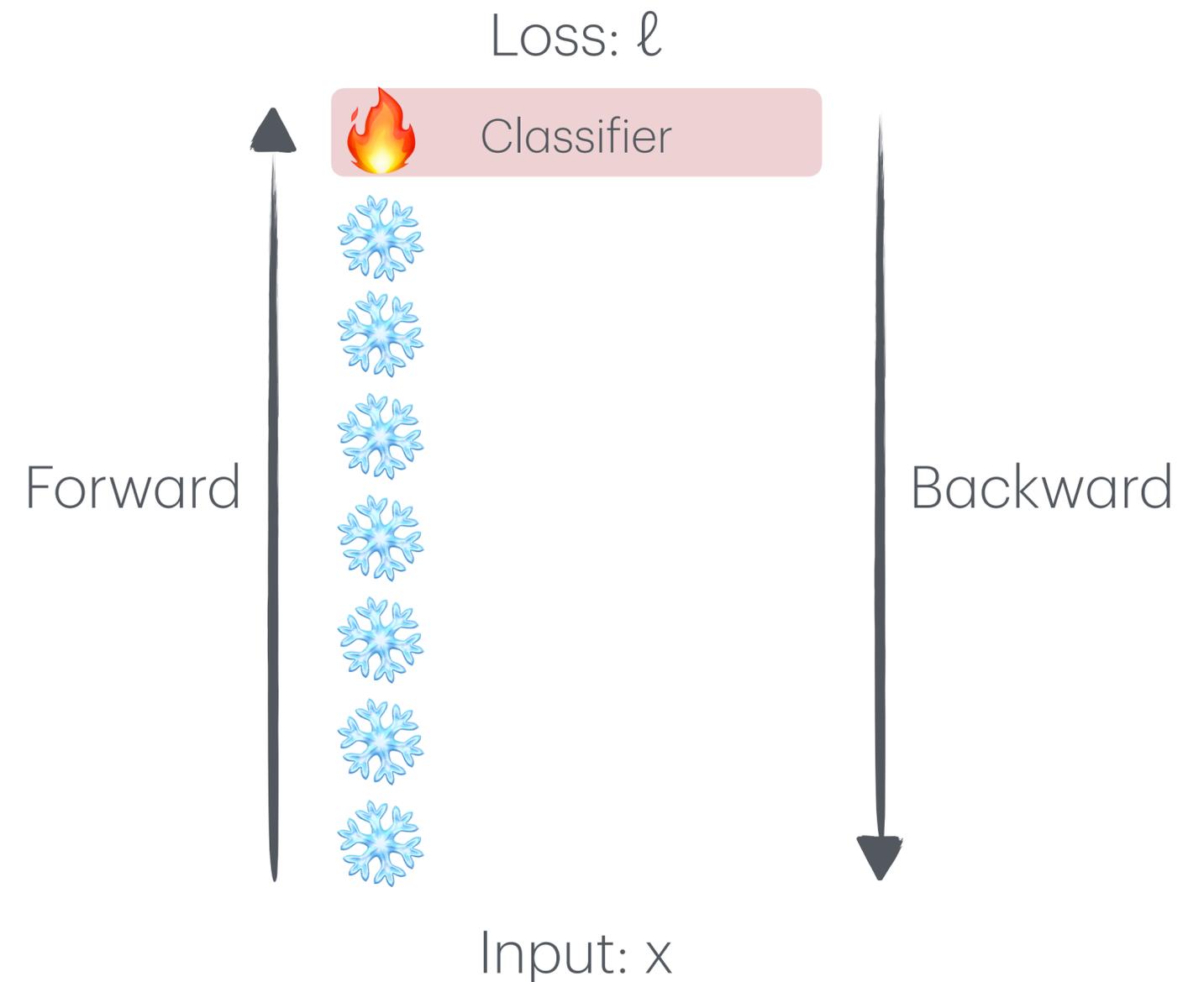
# Reducing Memory Use

- Idea: Train fewer parameters
  - Keep most parameters frozen
    - No gradient, no momentum
  - Train a small subset
    - With gradient and momentum



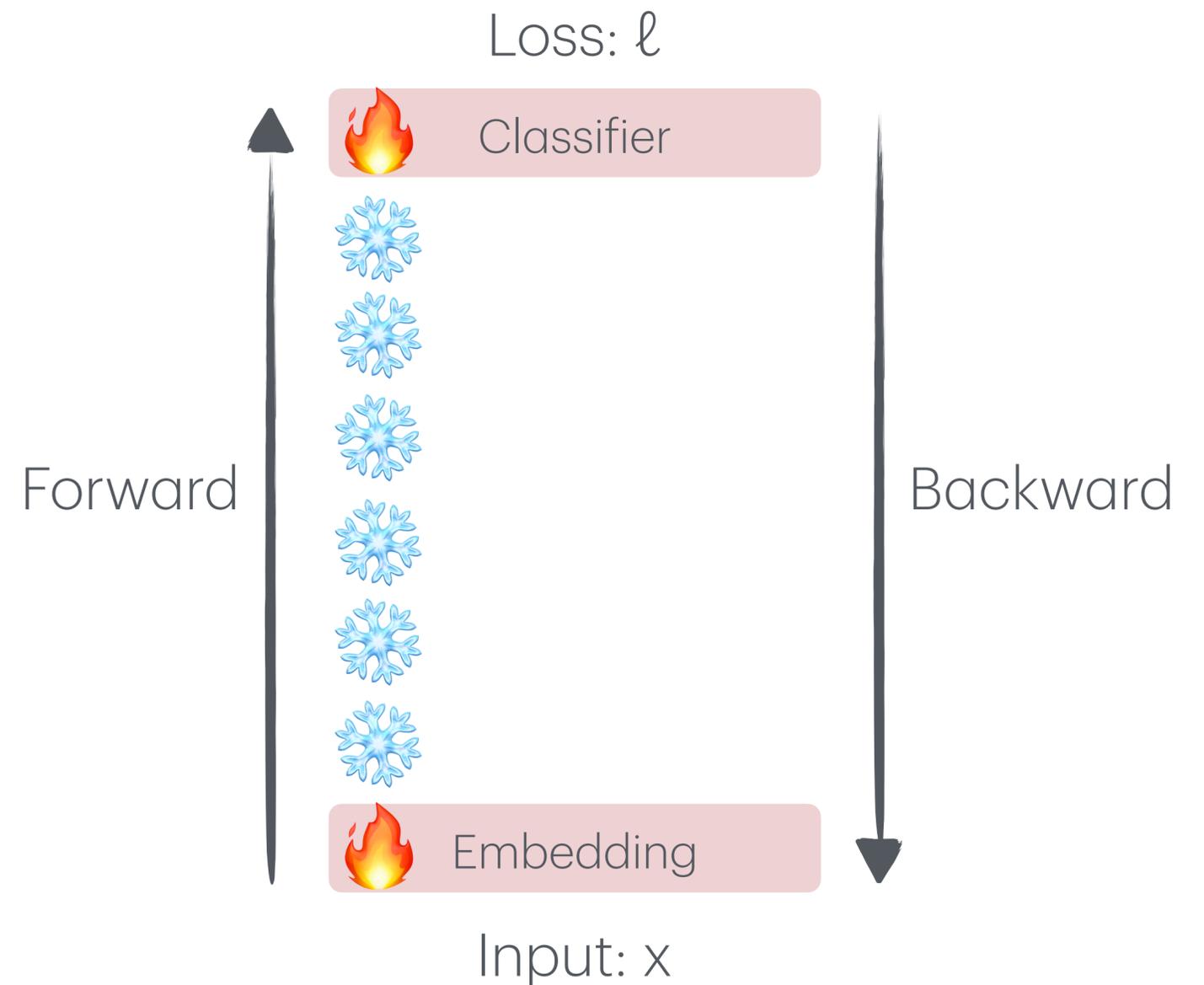
# Fine-tuning classifier

- Freeze backbone
- Train classifier
- Most memory efficient
  - No backprop
  - Very few learnable parameters
- Not very expressive



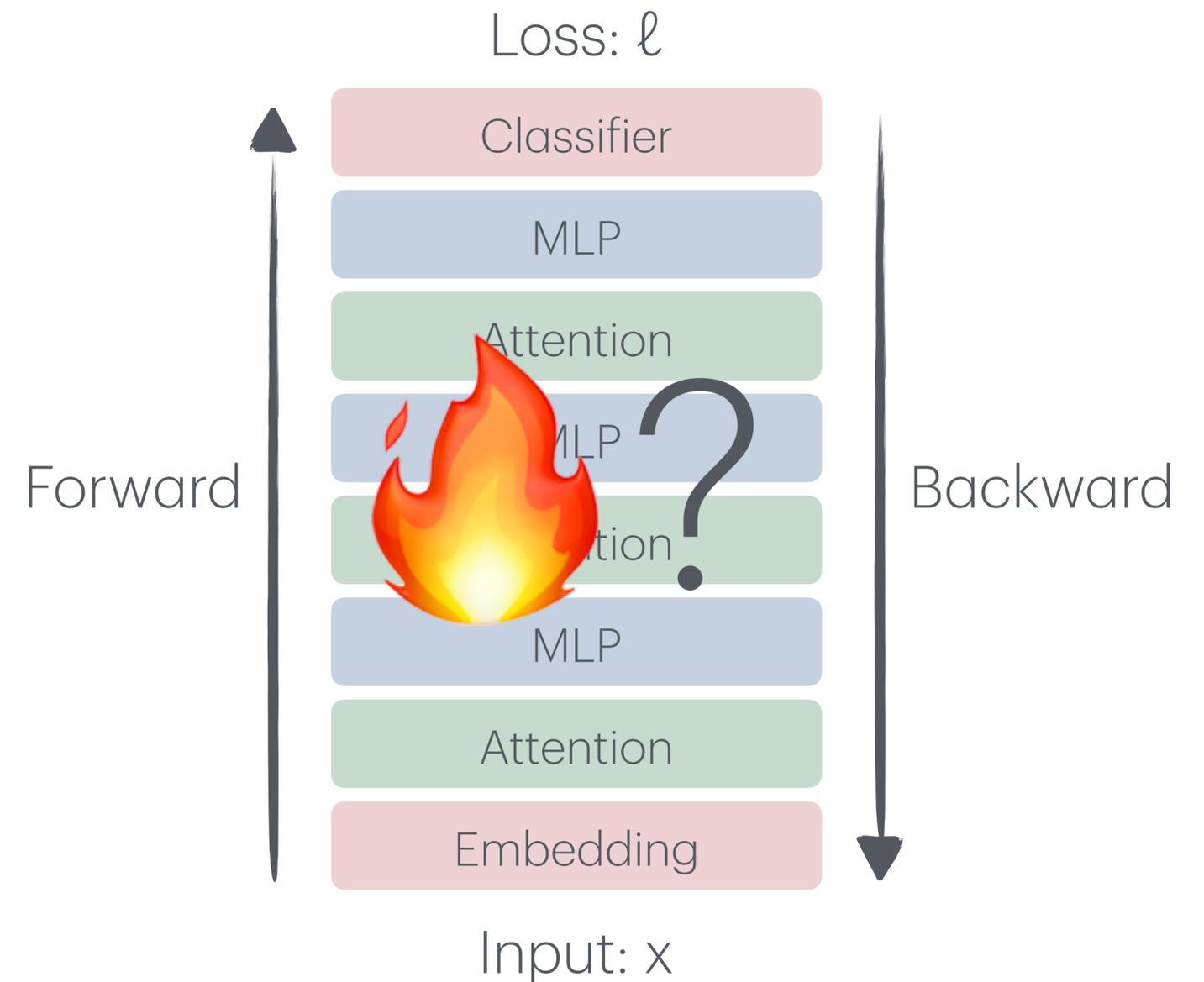
# Input adapters

- Freeze backbone
- Train input embedding (maybe classifier)
- Fairly memory efficient
  - Very few learnable parameters
- Popular with LLMs
  - Soft-prompting
  - Adapters for new inputs



# Intermediate layers

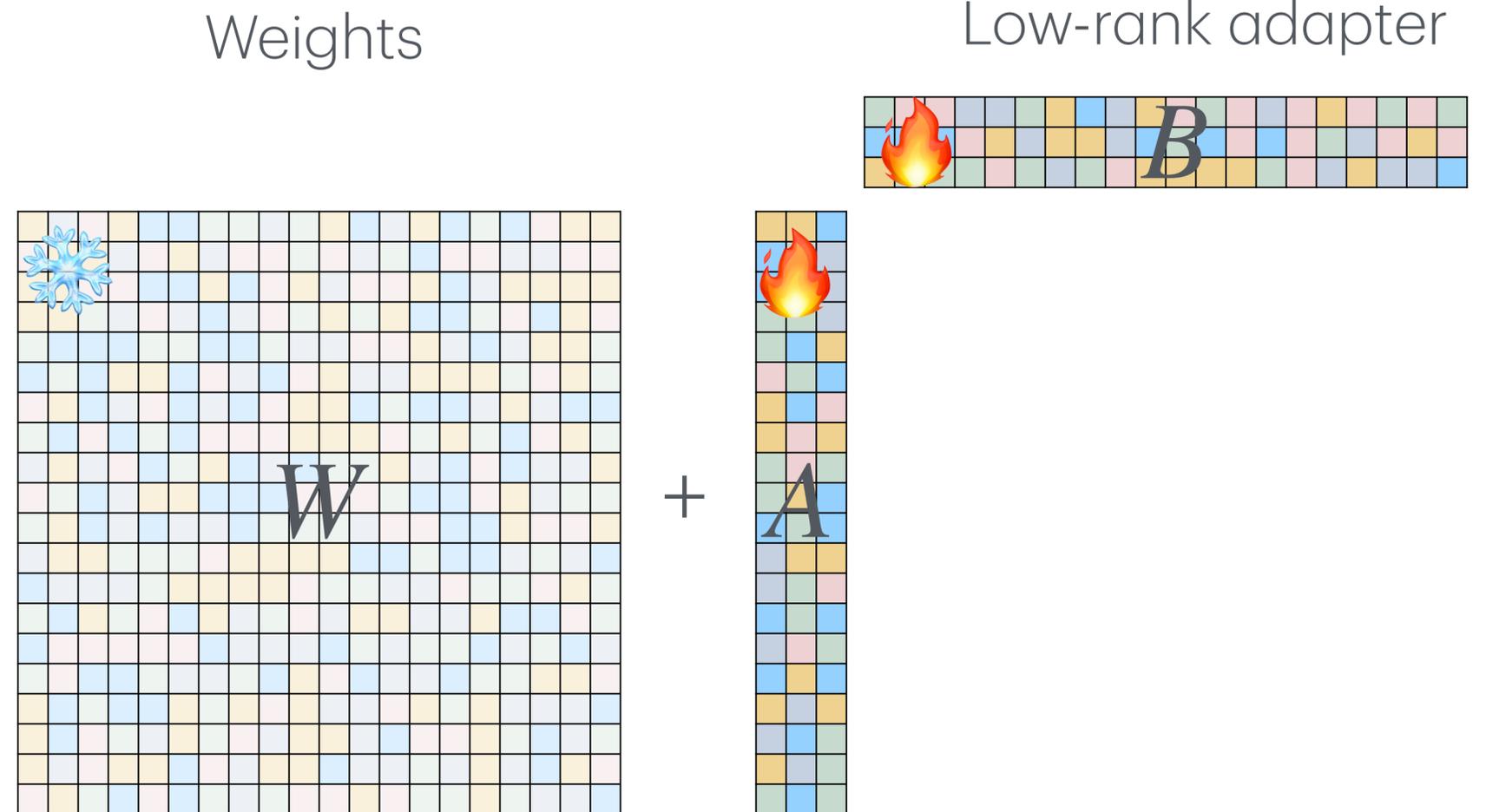
- Fine-tuning input and output does not change computation inside network significantly
- Cannot learn new “internal computation”
- Can we learn a subset of intermediate layer parameters?



# Low Rank Adapters

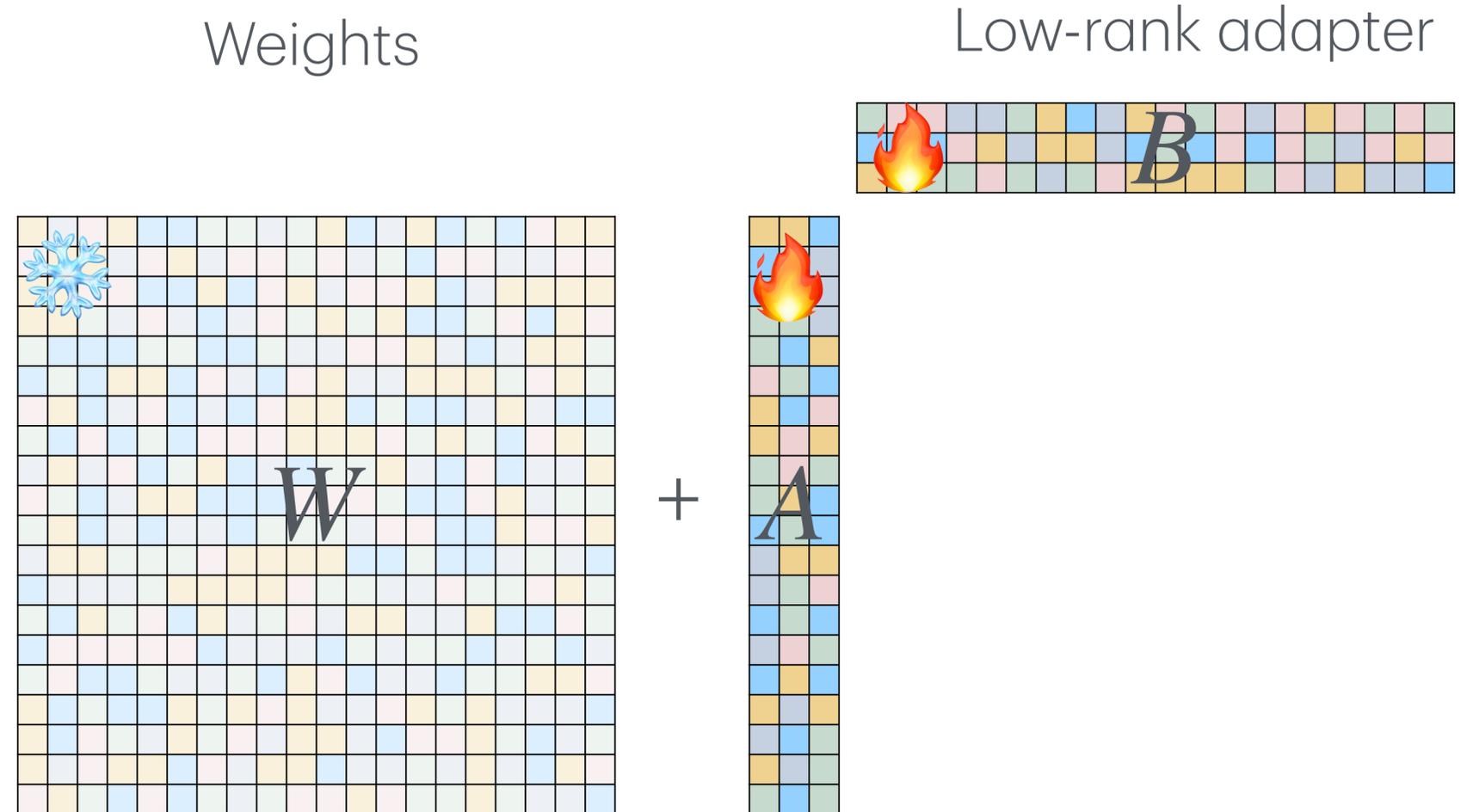
## LoRA

- Keep weights  $W \in \mathbb{R}^{N \times M}$  frozen
- Learn adapter  $AB$ 
  - $A \in \mathbb{R}^{N \times R}, B \in \mathbb{R}^{R \times M}$
  - Rank  $R \ll \min(M, N)$
- Total parameters:  $R(N + M)$



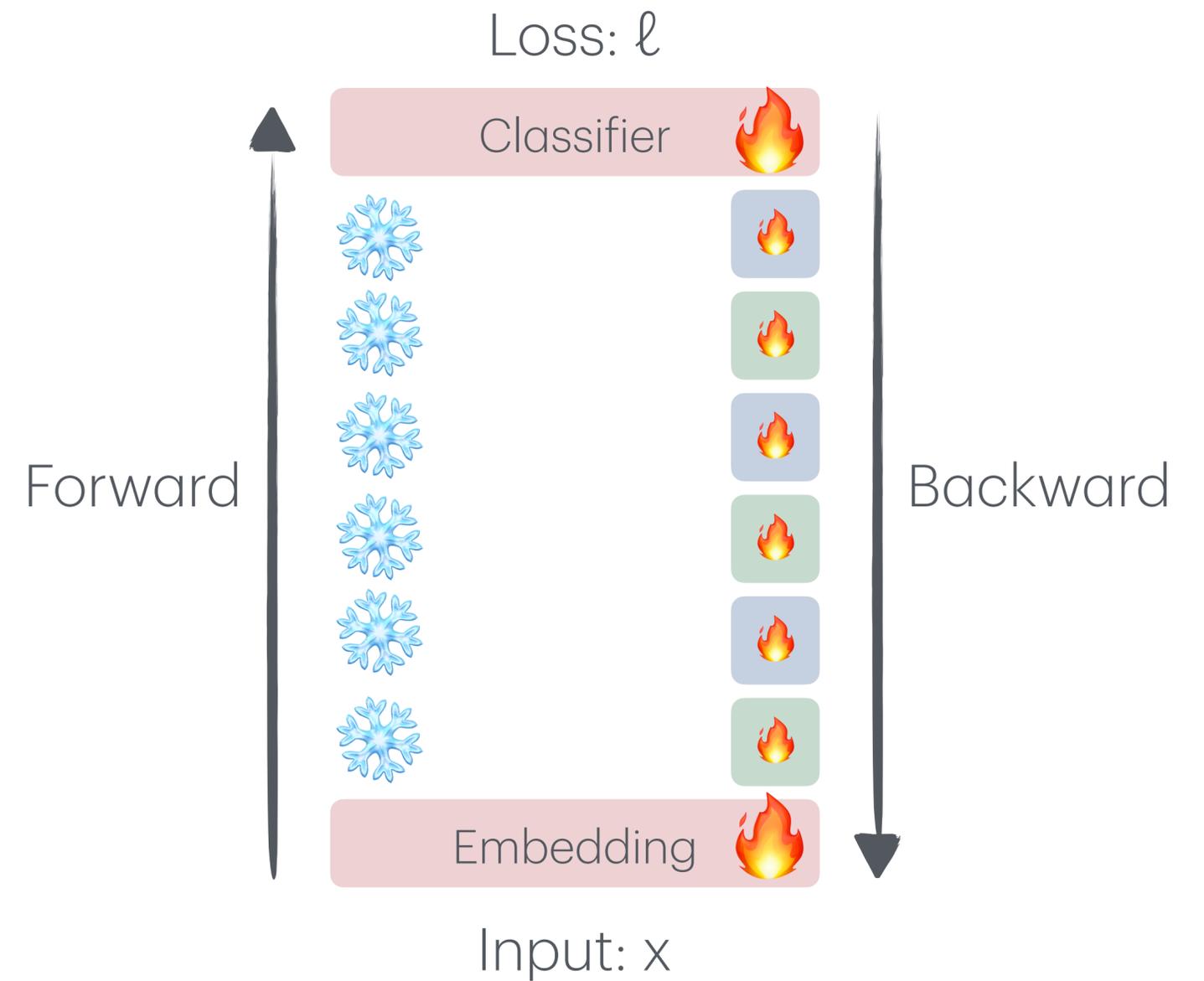
# Low Rank Adapters

- How do we train  $W$ ?
  - We use a pre-trained model
- How do we initialize  $A$  and  $B$ ?
  - $A$  small random (normal)
  - $B$  zero



# LoRA models

- Most weights frozen
- Train adapter for
  - All linear layers
  - Just MLPs
  - Just Attention
- Optionally train full input and output embedding



# LoRA in practice

- Download weights of a pre-trained model
- Define LoRALinear layer

$$Wx + b \rightarrow Wx + b + \alpha \frac{AB}{R}x$$

- Rewrite model with LoRALinear layers
  - If careful, `load_state_dict` just works

```
class LoRALinear(nn.Linear):
    def __init__(self, in_features: int, out_features: int, rank: int,
                 alpha: float, bias: bool = True, device=None,
                 dtype=None):
        super().__init__(in_features, out_features, bias, device, dtype)

        self.lora_a = nn.Linear(in_features, rank, bias=False,
                                device=device, dtype=dtype)
        self.lora_b = nn.Linear(rank, out_features, bias=False,
                                device=device, dtype=dtype)
        self.alpha_div_rank = alpha / rank

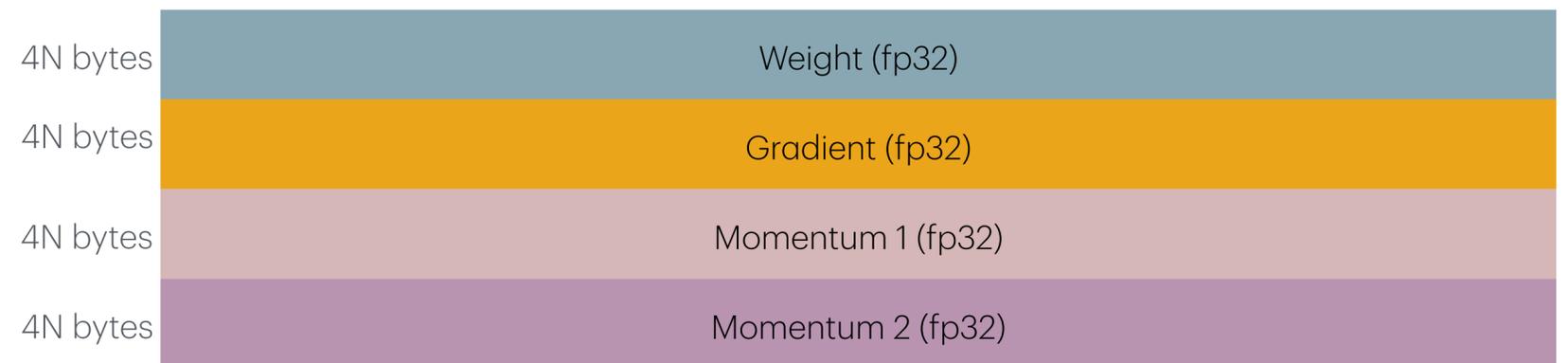
        nn.init.kaiming_uniform_(self.lora_a.weight)
        nn.init.zeros_(self.lora_b.weight)

    def forward(self, x: Tensor) -> Tensor:
        return super().forward(x) +
            self.alpha_div_rank / self.lora_b(self.lora_a(x))
```

# Training large models

## Memory requirements

- Without optimization:
  - Model parameters:  $N$
  - Weights:  $N$  floats
  - Gradients:  $N$  floats
  - Momentum:  $N$  floats
  - 2nd momentum (ADAM):  $N$  floats
- $16N$  bytes without counting activations



# Training LoRA models

## Memory requirements

- LoRA
  - Model parameters:  $N$ , LoRA param  $M$
  - Weights:  $N+M$  floats
  - Gradients:  $M$  floats
  - Momentum:  $M$  floats
  - 2nd momentum (ADAM):  $M$  floats
- $4N+16M$  bytes without activations
- $M$  often  $\sim 1-5\%$  of  $N$



# References

- [1] Edward J. Hu, et al. Lora: Low-rank adaptation of large language models. 2021 ([link](#))