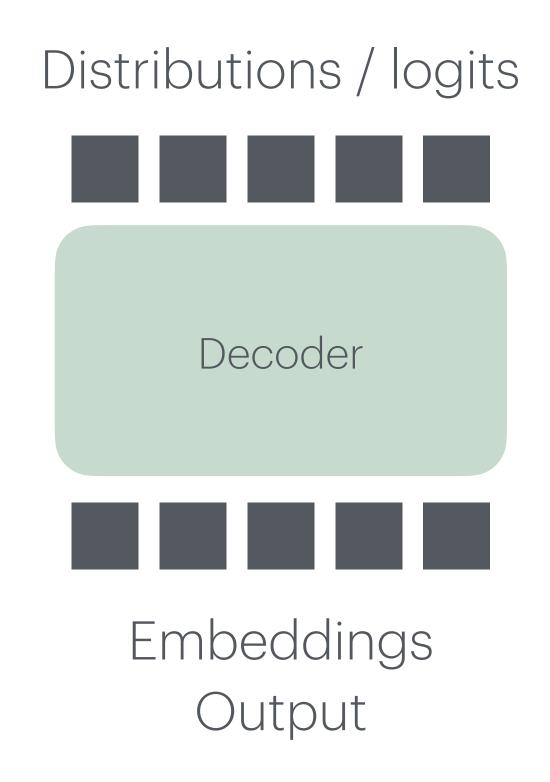
Direct Preference Optimization

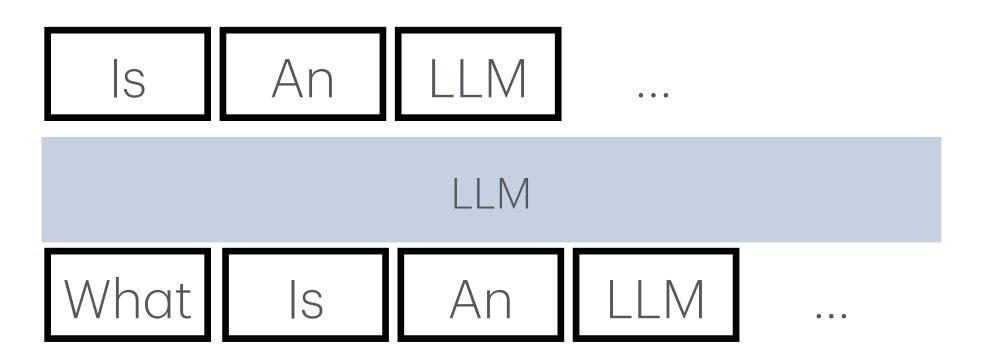
RLHF



Language Models

- Decoder-only LLMs
 - Modeling auto-regressive distribution over tokens
 - $P(\mathbf{t}) = P(t_1)P(t_2 | t_1)P(t_3 | t_1, t_2)P(t_4 | t_1...t_3)...$
- Generation / Sampling: $\mathbf{t} \sim P$





Instruction tuning

- Teach a LLM to follow a certain template in answering
 - Tell LLM what to do
 - Does not tell LLM what not to do

> I want to refocus my diet on only eating Apples and supplements.

Let me provide information on how to make the most of eating apples as a primary food source.

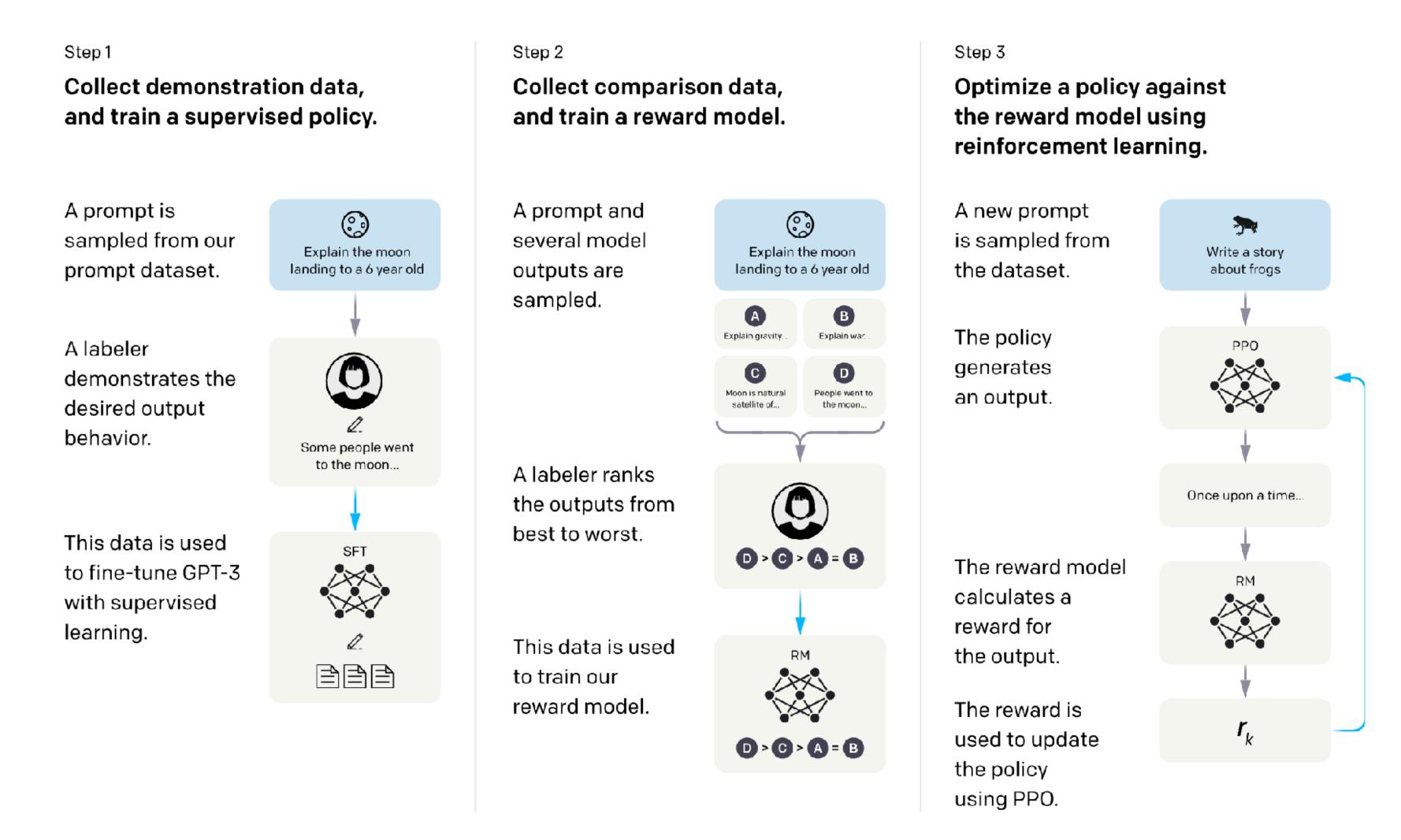
**Apple selection: ** Focus on eating a variety of apples to ensure you get a range of nutrients. Some apple varieties are higher in certain nutrients than others. For example:

- * Granny Smith and Braeburn apples have more malic acid, which can help with digestion.
- * Gala and Fuji apples contain more vitamins A and C.

•••

RLHF

Reinforcement Learning from Human Feedback



RLHF - a recap

. Learn reward: $\mathcal{E} = E_{x,y_+,y_-} \left[\log \sigma \left(r(x,y_+) - r(x,y_-) \right) \right]$

. Optimize: $E_{y \sim P(\cdot|x)} \left[(r(y,x)) \nabla \log P(y|x) \right] - \beta D_{KL} \left[P(y|x) | P_{ref}(y|x) \right]$

. Learn reward: $\mathcal{E} = E_{x,y_+,y_-} \left[\log \sigma \left(r(x,y_+) - r(x,y_-) \right) \right]$

. Optimize: $E_{y \sim P(\cdot|x)} \left[(r(y,x)) \nabla \log P(y|x) \right] - \beta D_{KL} \left[P(y|x) | P_{ref}(y|x) \right]$

. Closed form solution:
$$P(y \mid x) = \frac{1}{Z(x)} P_{ref}(y \mid x) \exp\left(\frac{1}{\beta} r(x, y)\right)$$

. Learn reward: $\mathcal{E} = E_{x,y_+,y_-} \left[\log \sigma \left(r(x,y_+) - r(x,y_-) \right) \right]$

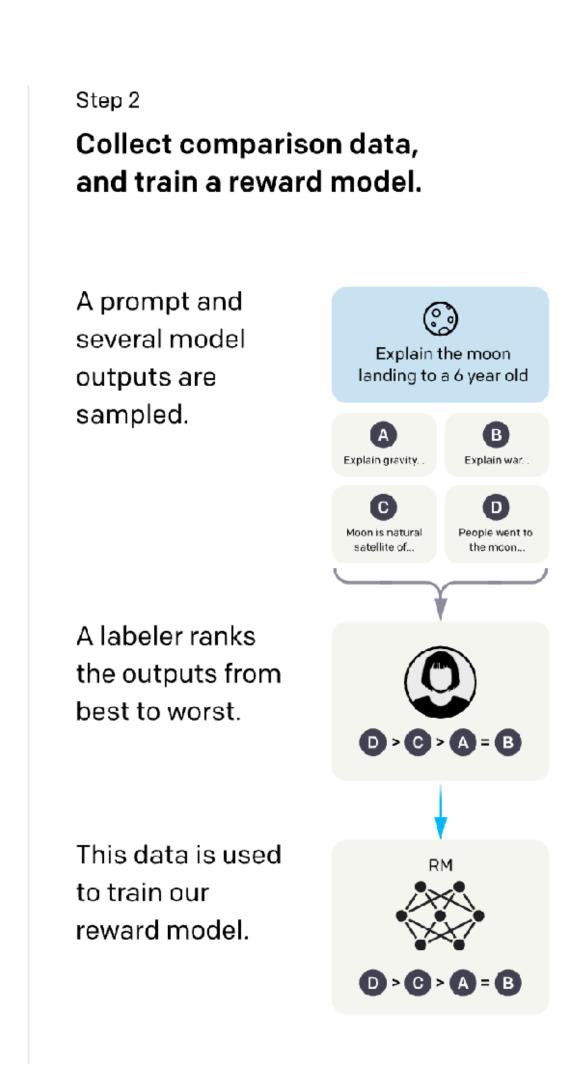
- . Optimize: $E_{y \sim P(\cdot \mid x)} \left[(r(y, x)) \nabla \log P(y \mid x) \right] \beta D_{KL} \left[P(y \mid x) \mid P_{ref}(y \mid x) \right]$
 - . Closed form solution: $P(y \mid x) = \frac{1}{Z(x)} P_{ref}(y \mid x) \exp\left(\frac{1}{\beta} r(x, y)\right)$

$$r(x,y) = \beta \frac{P(y|x)}{P_{ref}(y|x)} + \beta \log Z(x)$$

- . Learn reward: $\ell = E_{x,y_+,y_-} \left[\log \sigma \left(r(x,y_+) r(x,y_-) \right) \right]$
 - Closed form $\mathcal{C}_{DPO} = E_{x,y_+,y_-} \left[\log \sigma \left(\beta \frac{rP(x,y_+)}{P_{ref}(x,y_+)} \beta \frac{rP(x,y_-)}{P_{ref}(x,y_-)} \right) \right]$
- . Optimize: $E_{y \sim P(\cdot|x)} \left[(r(y,x)) \nabla \log P(y|x) \right] \beta D_{KL} \left[P(y|x) | P_{ref}(y|x) \right]$
 - . Closed form solution: $P(y \mid x) = \frac{1}{Z(x)} P_{ref}(y \mid x) \exp\left(\frac{1}{\beta} r(x, y)\right)$
 - $r(x,y) = \beta \frac{P(y|x)}{P_{ref}(y|x)} + \beta \log Z(x)$

$$\mathcal{E}_{DPO} = E_{x,y_{+},y_{-}} \left[\log \sigma \left(\beta \frac{rP(x,y_{+})}{P_{ref}(x,y_{+})} - \beta \frac{rP(x,y_{-})}{P_{ref}(x,y_{-})} \right) \right]$$

- Closed form solution to reward models
 + RL
 - Supervised learning
 - Easy to implement
 - Efficient



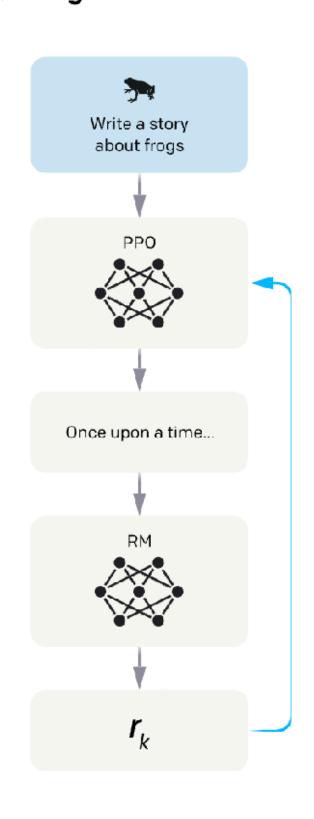
Optimize a policy against the reward model using reinforcement learning.

A new prompt is sampled from the dataset.

The policy generates an output.

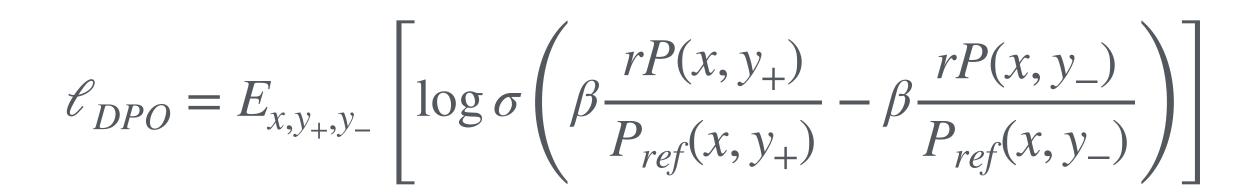
The reward model calculates a reward for the output.

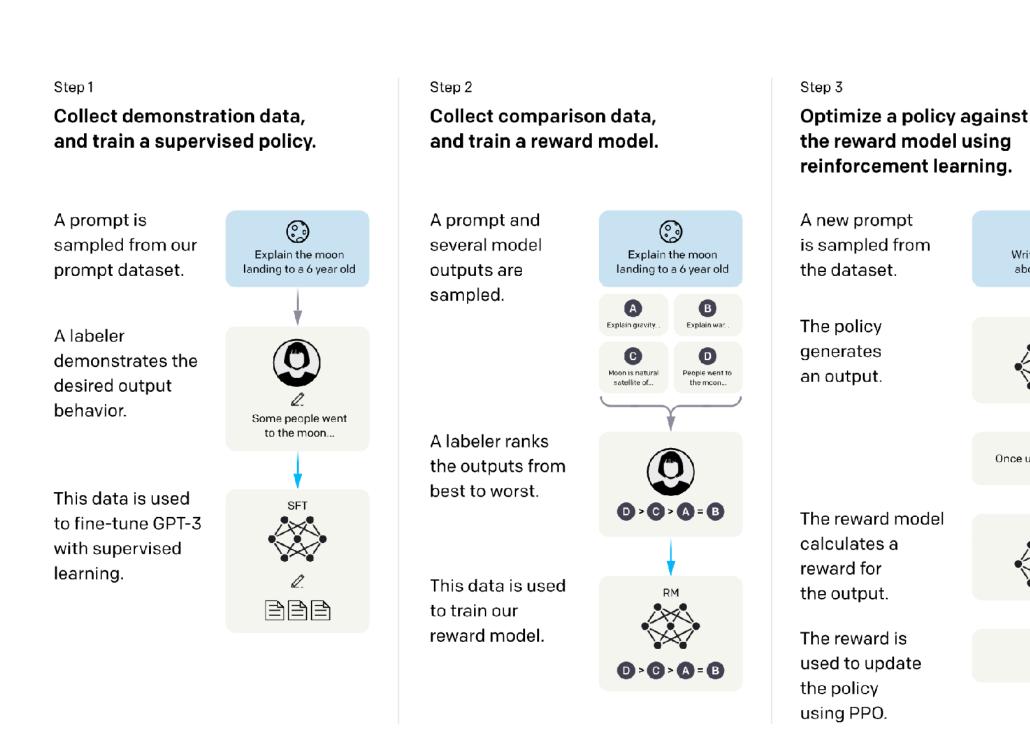
The reward is used to update the policy using PPO.



DPO vs RLHF

- DPO
 - Easier to make work
 - Can only learn on preference data
 - Generally produces long outputs
- RLHF
 - Requires quite a bit of RL knowledge
 - Higher ceiling (can use smaller preference data, larger fine-tuning data)





7

Write a story

Once upon a time.

Full Picture



References

- [1] Training language models to follow instructions with human feedback. Ouyang etal 2022.
- [2] Direct Preference Optimization: Your Language Model is Secretly a Reward Model, Rafailov et al 2023.