

Generation

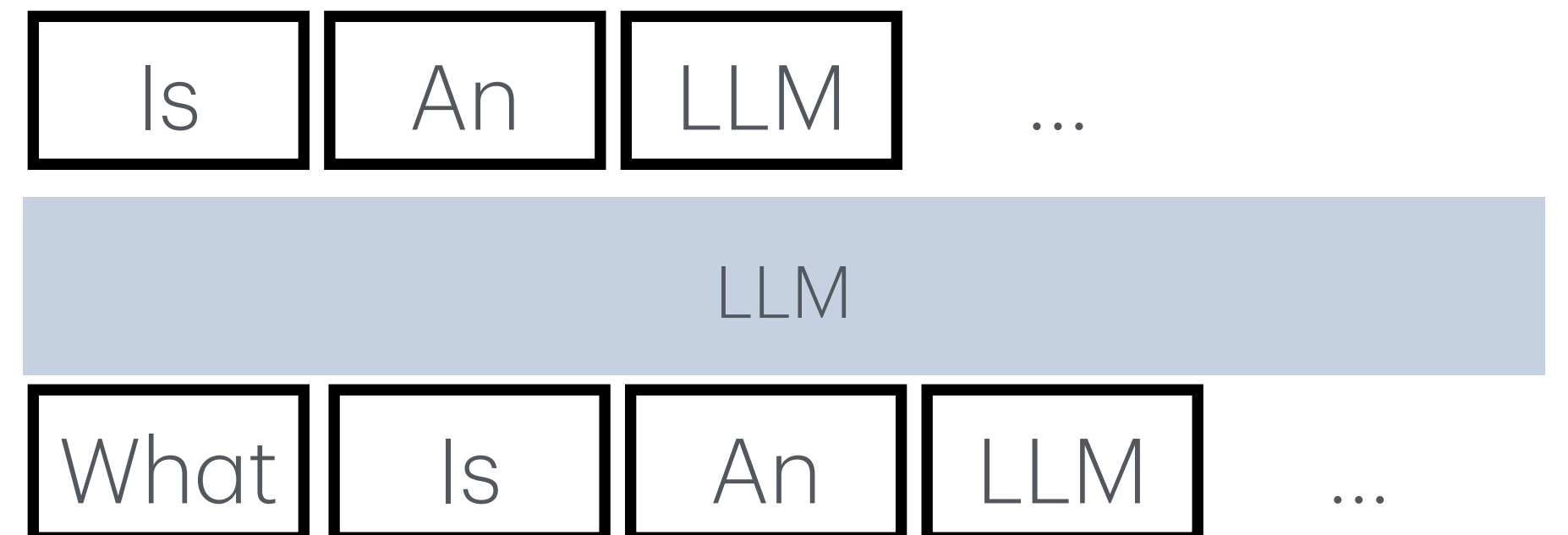
Language Models

- Decoder-only LLMs
 - Modeling auto-regressive distribution over tokens
 - $P(\mathbf{t}) = P(t_1)P(t_2 | t_1)P(t_3 | t_1, t_2)P(t_4 | t_1 \dots t_3) \dots$

Distributions / logits



Embeddings
Output



Language Models

Sampling

- How to generate text \mathbf{t} from P

Distributions / logits



Embeddings
Output

Is An LLM ...

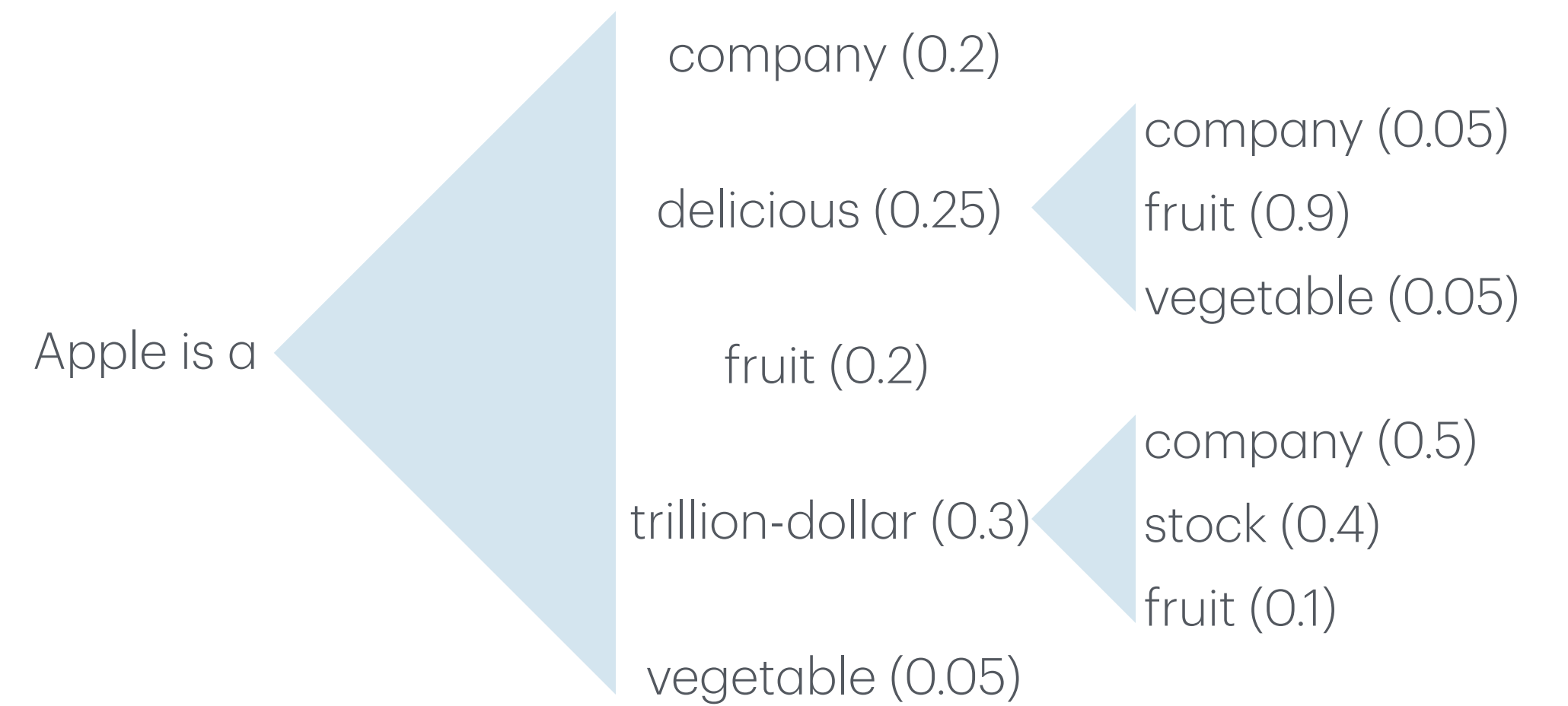


What Is An LLM ...

$$P(\mathbf{t}) = P(t_1)P(t_2 | t_1)P(t_3 | t_1, t_2)P(t_4 | t_1 \dots t_3) \dots$$

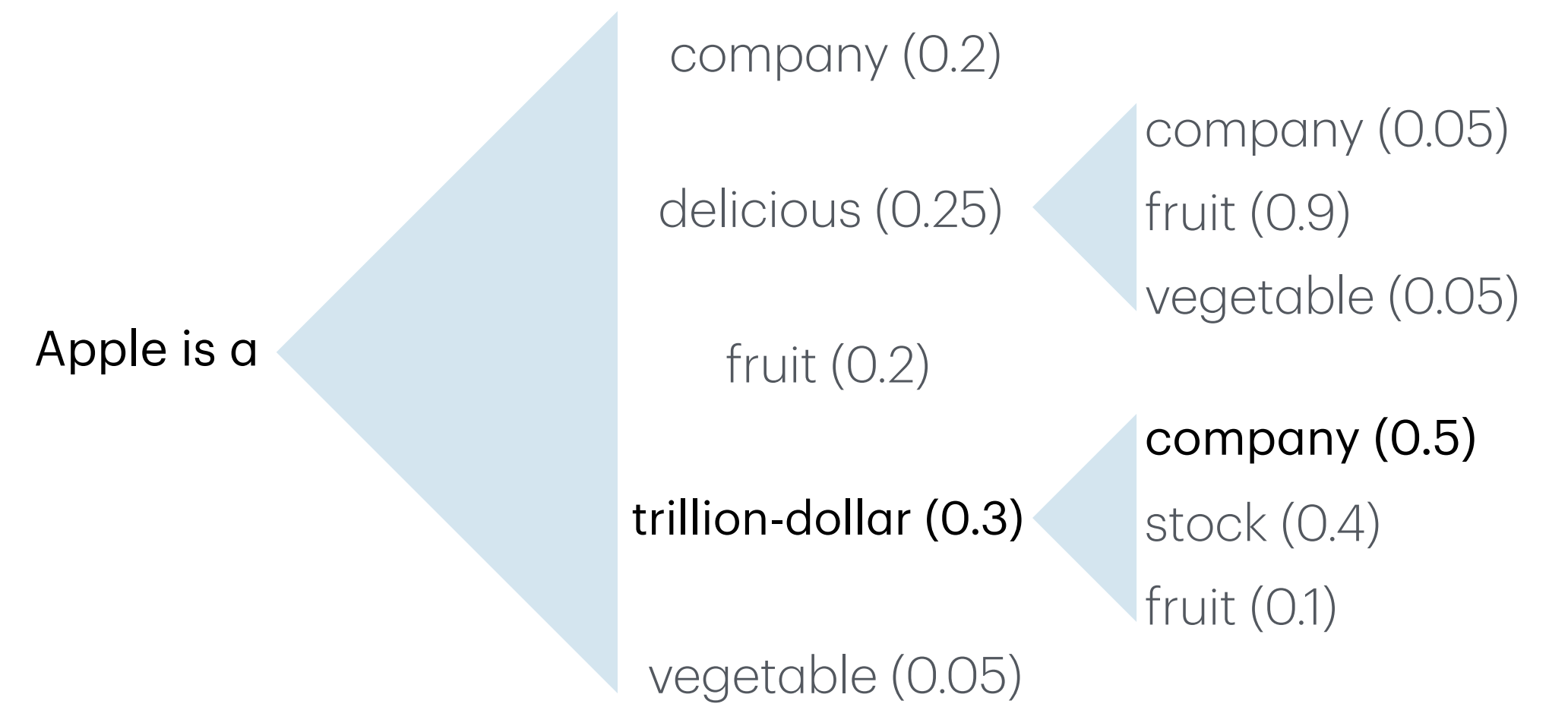
Generation

- LLM produces distribution over tokens
 - Exponentially large output space
- Tension between
 - Generalization (not assigning prob=0)
 - Fidelity (odd low-probability outputs)



Sampling - Greedy search

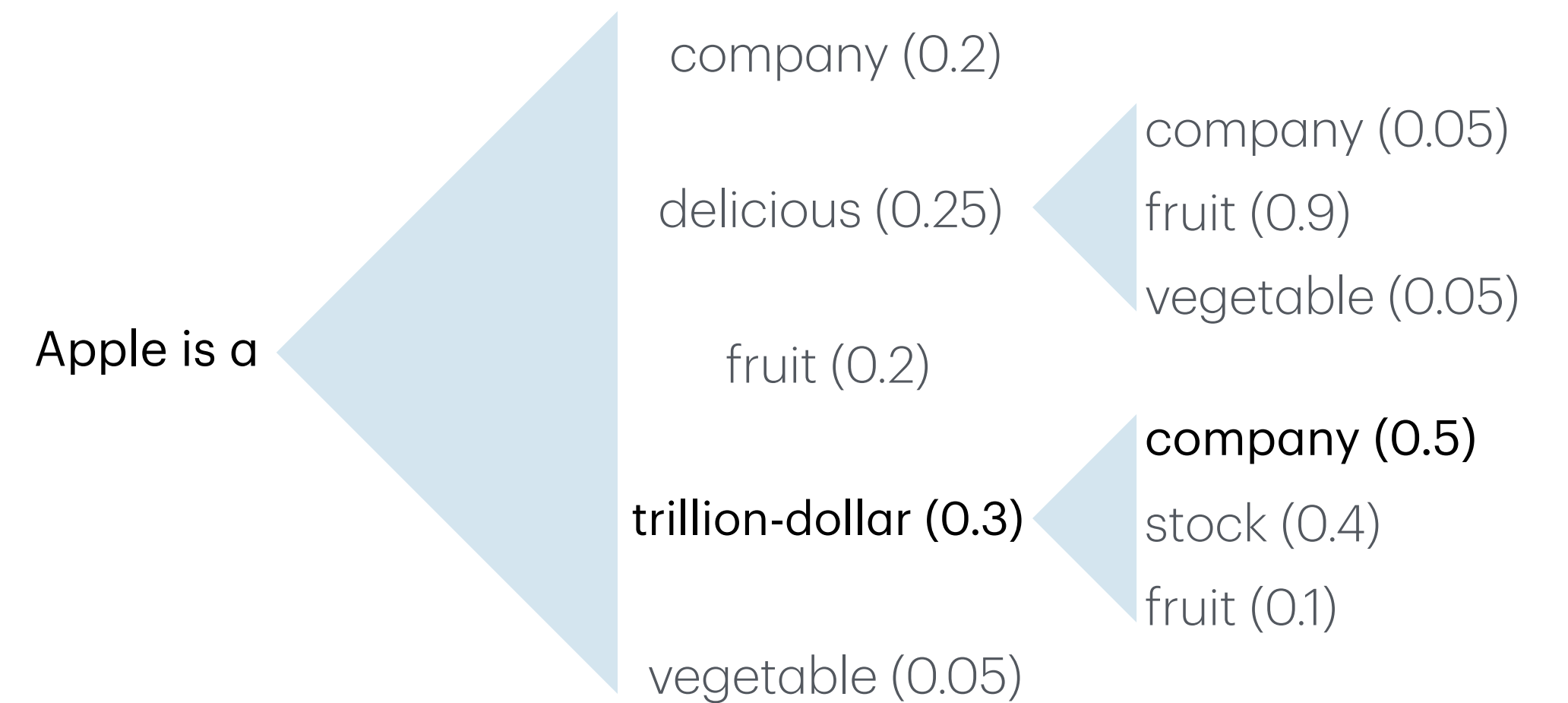
- Pick highest probability token next



Sampling - Greedy search

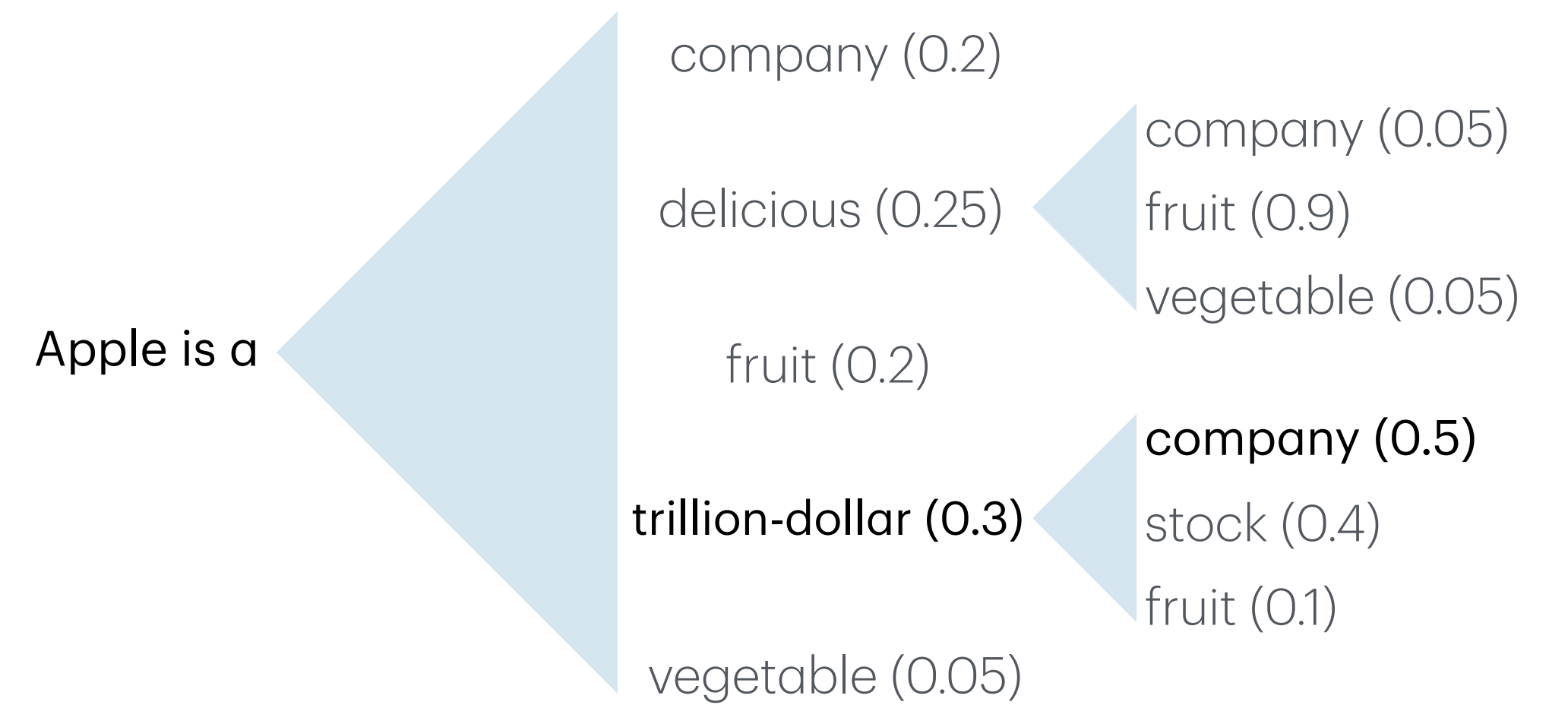
- A demo
ollama run llama3.1:greedy

```
FROM llama3.1:8b-text-q4_0  
PARAMETER temperature 0  
PARAMETER top_k 1000  
PARAMETER top_p 1.0
```



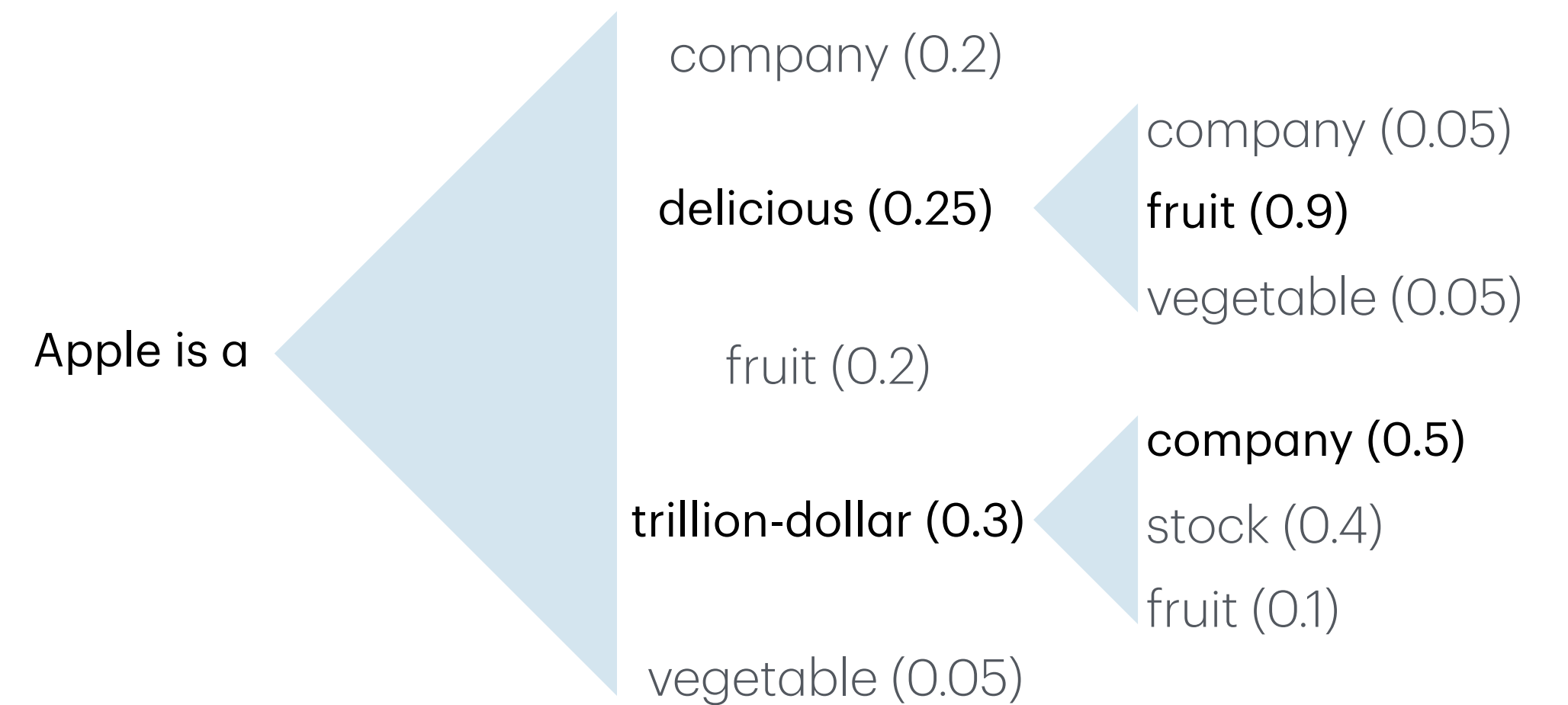
Sampling - Greedy search

- Pick highest probability token next
- 😊 Super simple
- 😊 Computationally efficient
- 😞 Single sequence
- 😞 Bad local decisions



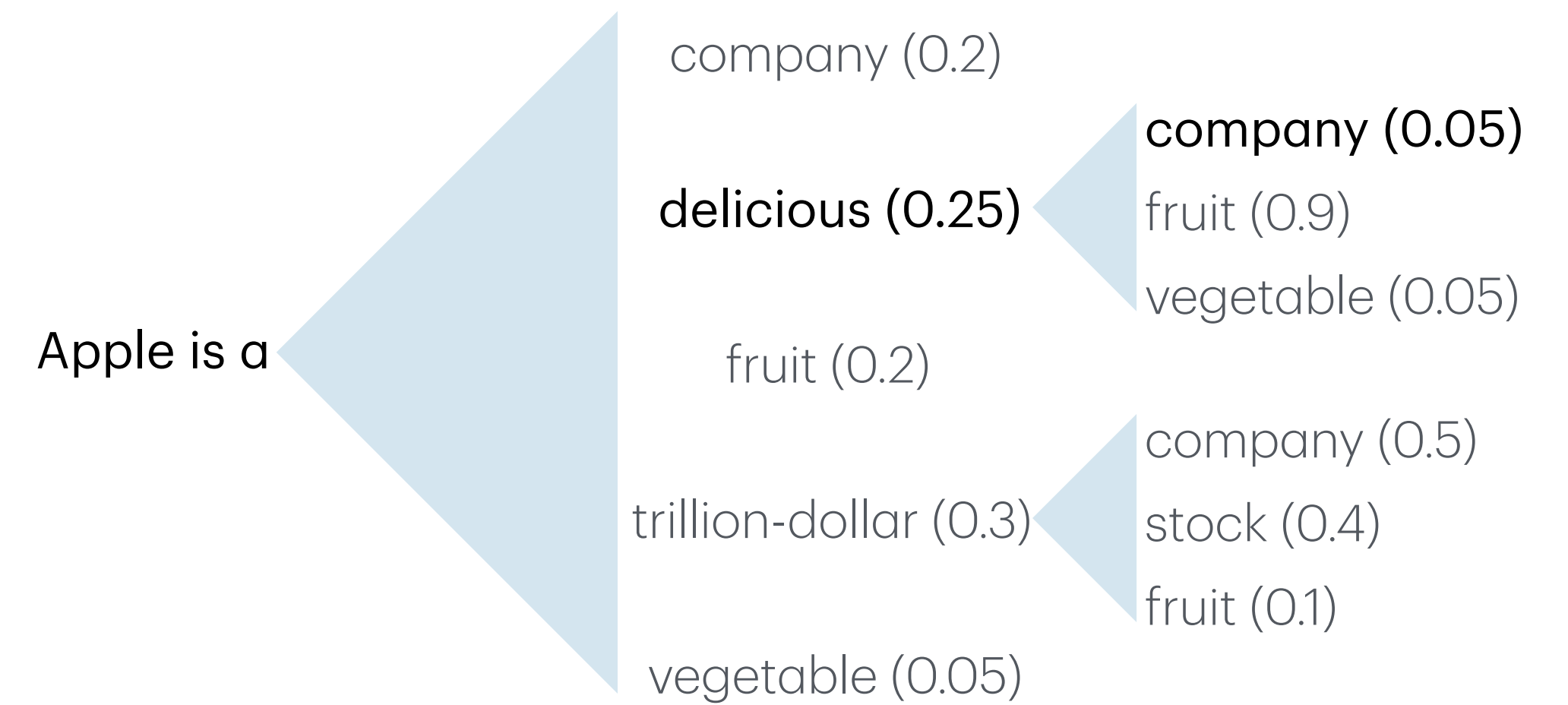
Sampling - Beam search

- Keep k-best samples around
 - Expand all, filter according to prob
- 😊 Good optimization
- 😞 Computationally more expensive
- 😞 Hard to define sampling objective



Sampling - Random sampling

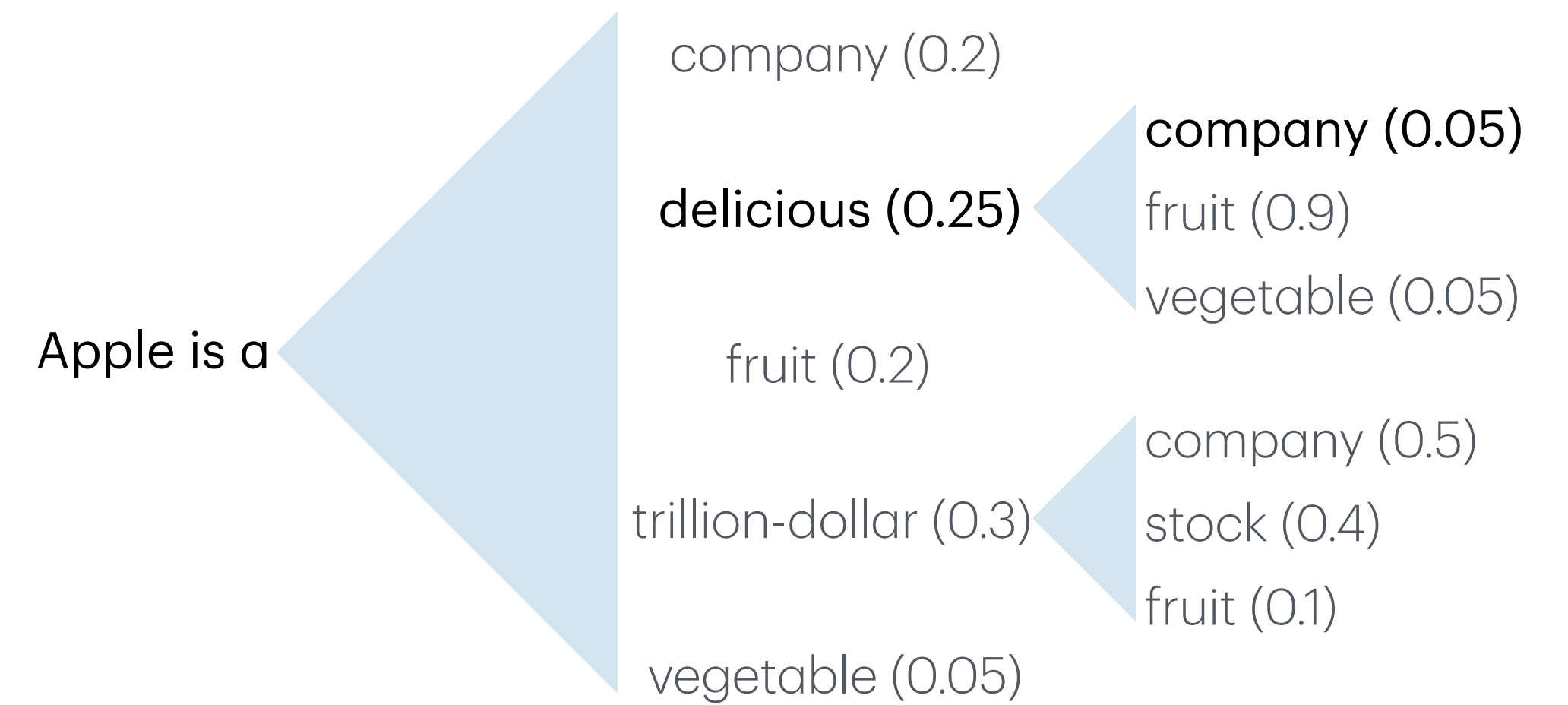
- Sample next word/token according to model distribution
- Samples follow exponentially large model distribution



Sampling - Random sampling

- A demo
ollama run llama3.1:temp1_random

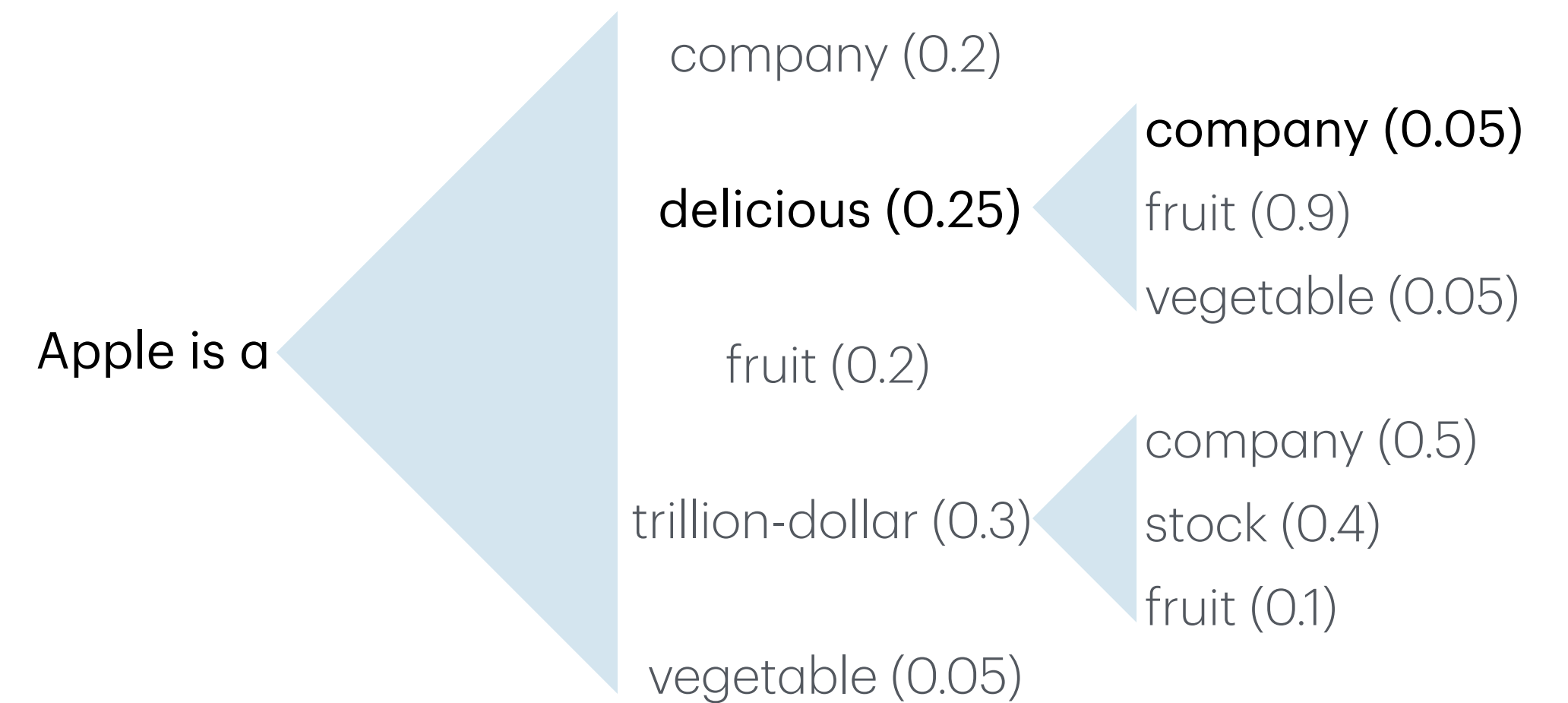
```
FROM llama3.1:8b-text-q4_0  
PARAMETER temperature 1  
PARAMETER top_k 1000  
PARAMETER top_p 1.0
```



Sampling - Random sampling

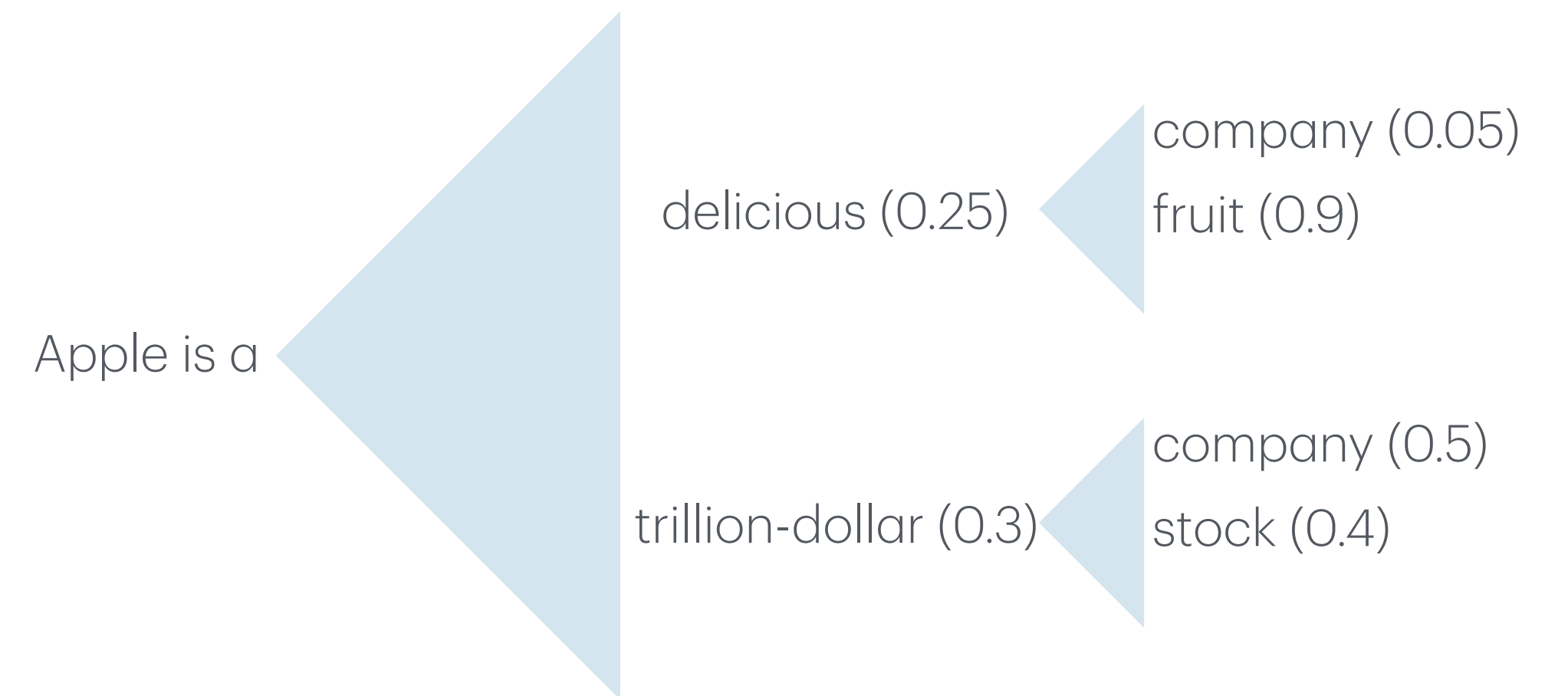
- Sample next word/token according to model distribution
- Samples follow exponentially large model distribution

- 😊 Samples sound human-like
- 😊 Computationally efficient
- 😞 Sampling low-prob transitions



Sampling - Top-K sampling

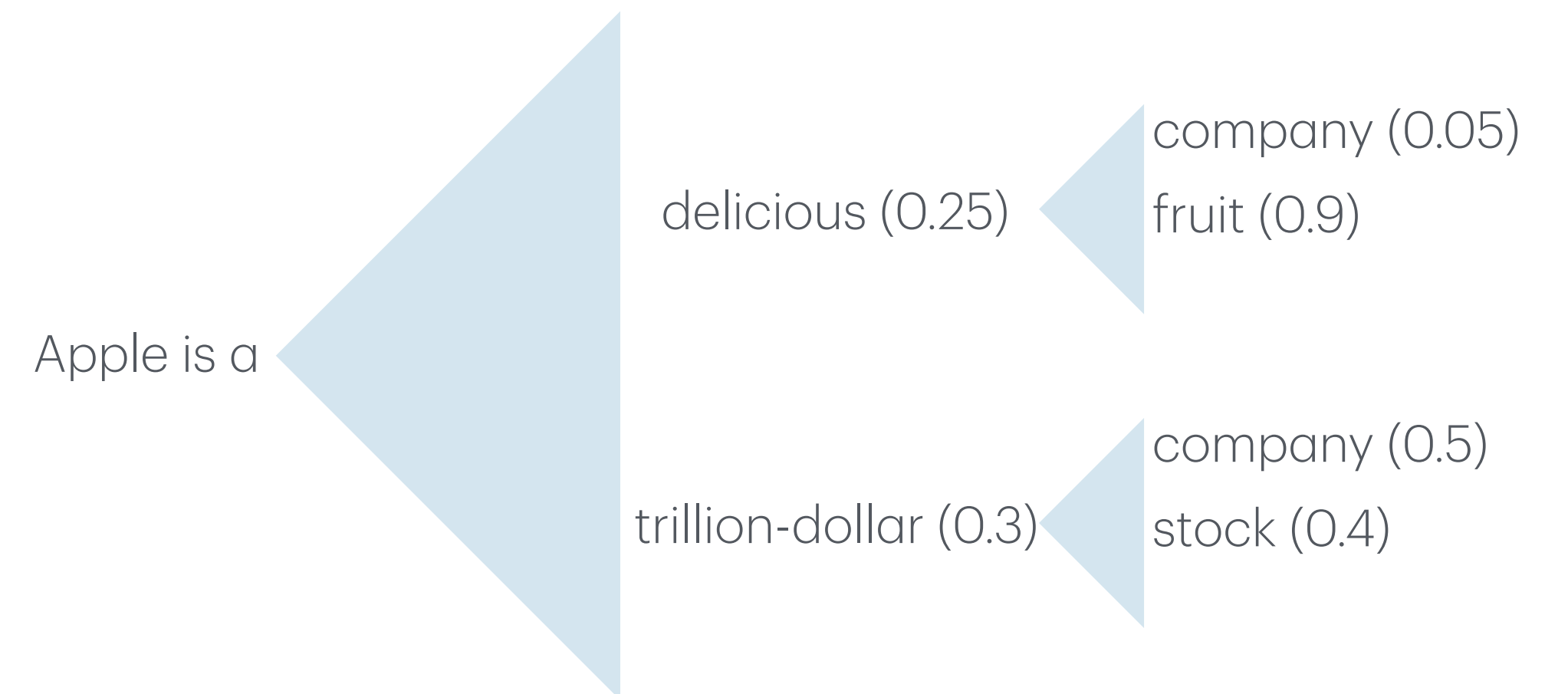
- Random sampling
- Only consider k-most likely options



Sampling - Top-K sampling

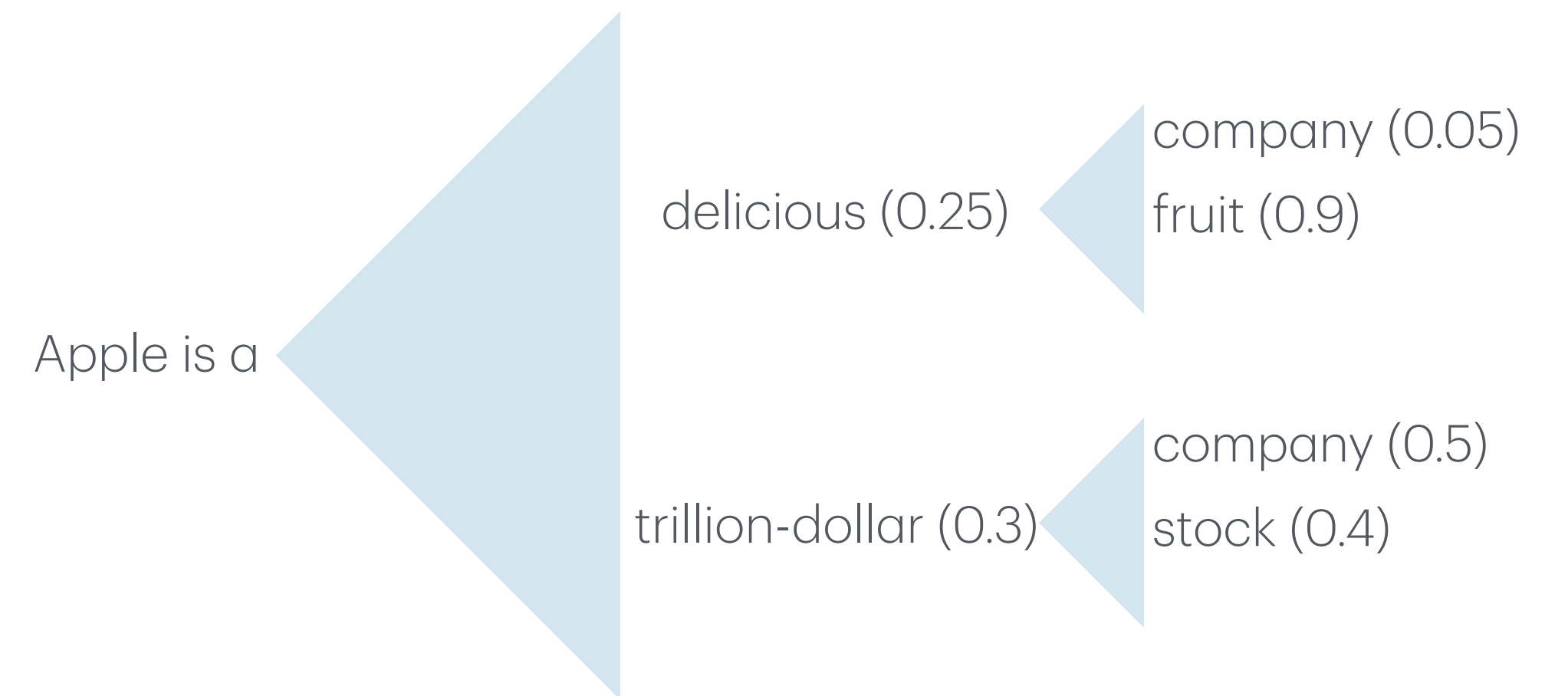
- A demo
ollama run llama3.1:top10

```
FROM llama3.1:8b-text-q4_0  
PARAMETER temperature 1  
PARAMETER top_k 10  
PARAMETER top_p 1.0
```



Sampling - Top-K sampling

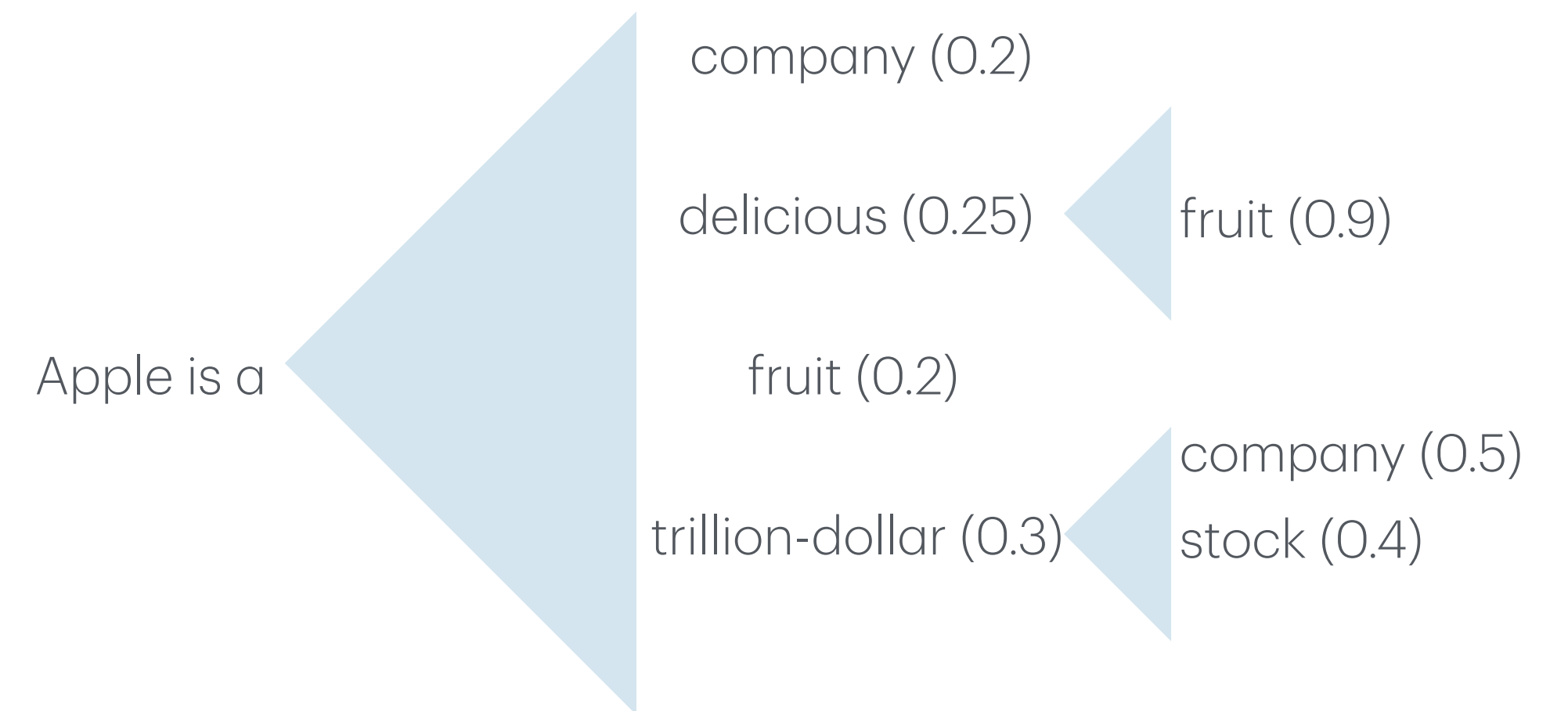
- Random sampling
 - Only consider k-most likely options
- 😊 Samples sound human-like
- 😊 Sampling fewer low-prob transitions
- 😞 k is hard to set (context dependent)



Sampling - Nucleus sampling

Top-p

- Random sampling
 - Ignore p least likely percentile



Sampling - Nucleus sampling

Top-p

- A demo
ollama run llama3.1:top-p

```
FROM llama3.1:8b-text-q4_0  
PARAMETER temperature 1  
PARAMETER top_k 1000  
PARAMETER top_p 0.9
```

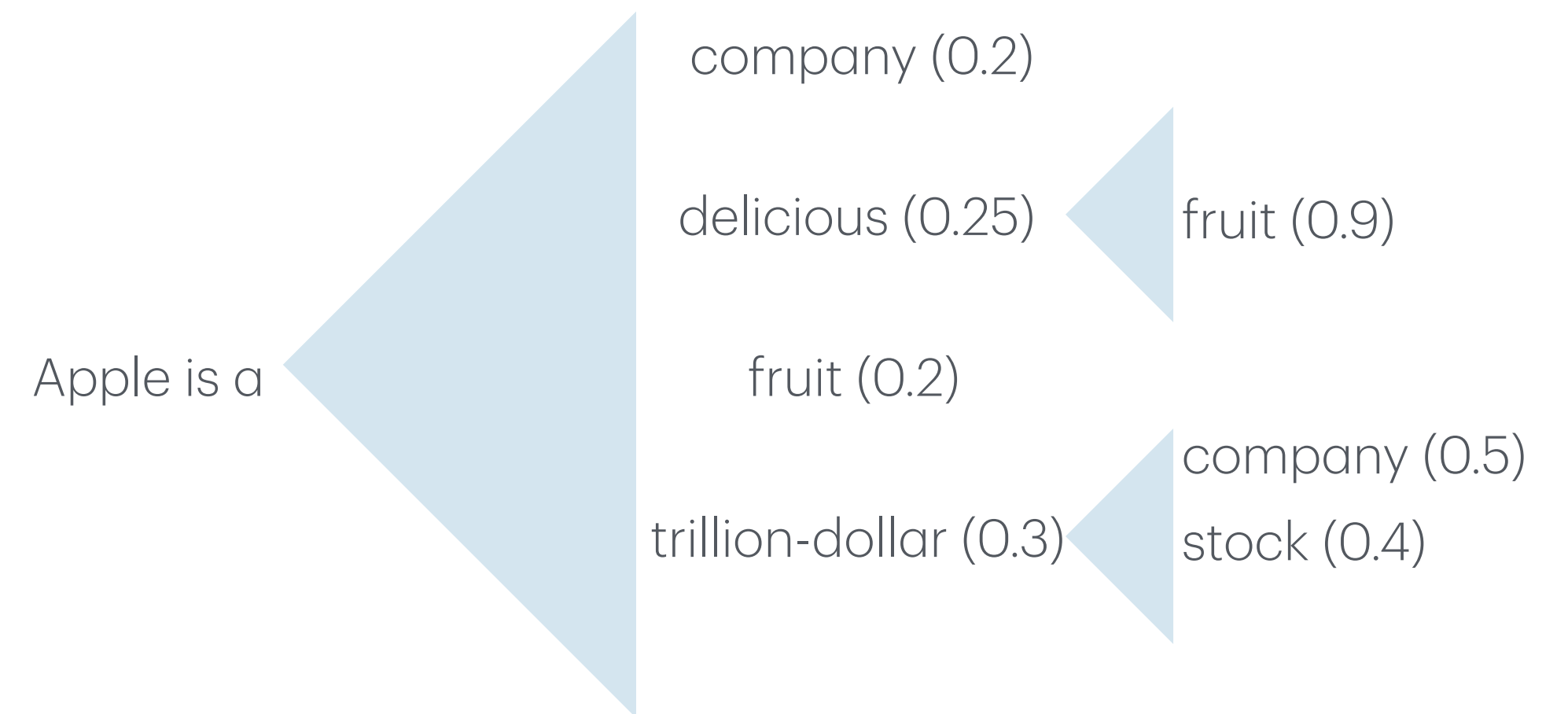


Sampling - Nucleus sampling

Top-p

- Random sampling
 - Ignore p least likely percentile
- 😊 Samples sound human-like
- 😊 Sampling fewer low-prob transitions

- Used almost everywhere



Sampling - Min-P

- Random sampling
- Ignore $p < \alpha p_{\max}$



Sampling - Min-P

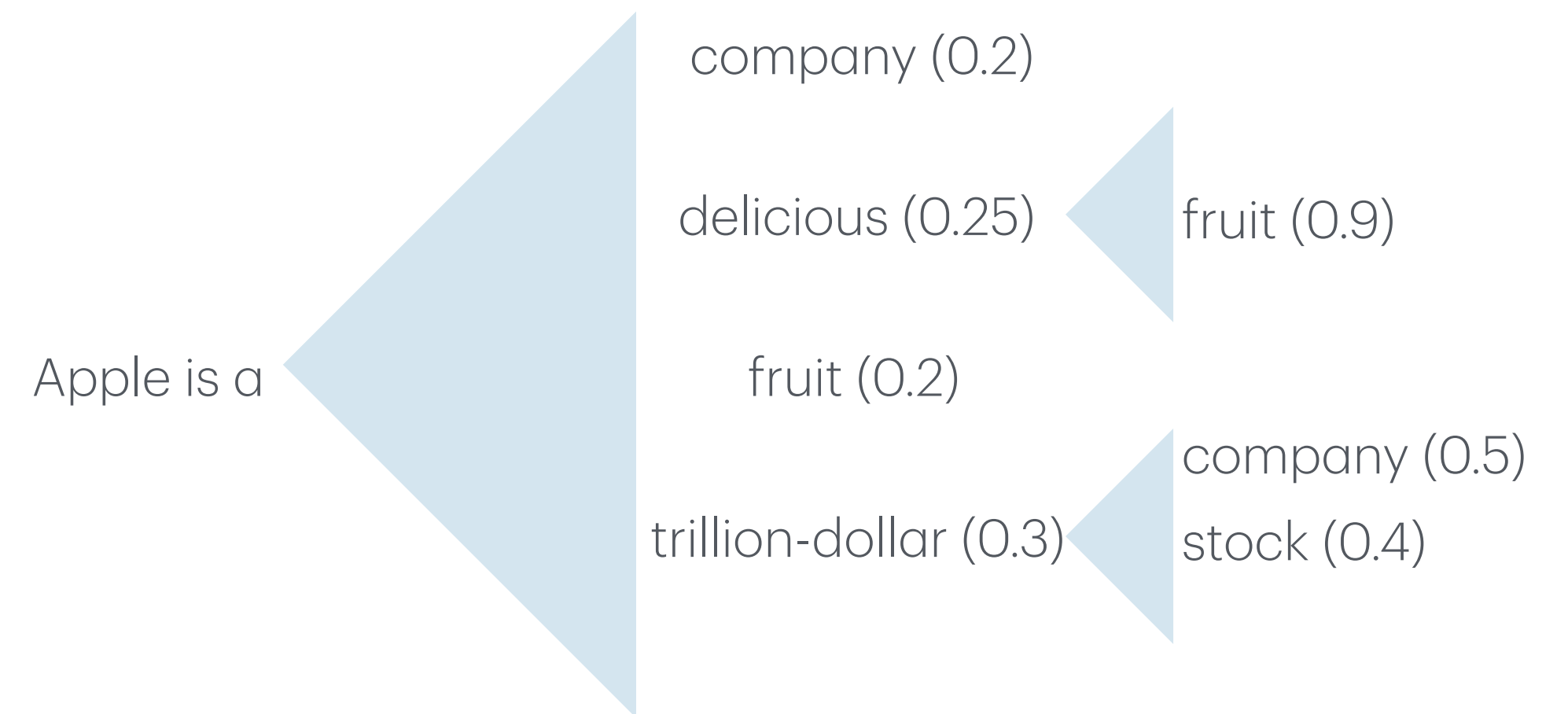
- A demo
ollama run llama3.1:min-p

```
FROM llama3.1:8b-text-q4_0
PARAMETER temperature 1
PARAMETER top_k 1000
PARAMETER top_p 1.0
PARAMETER min_p 0.1
```



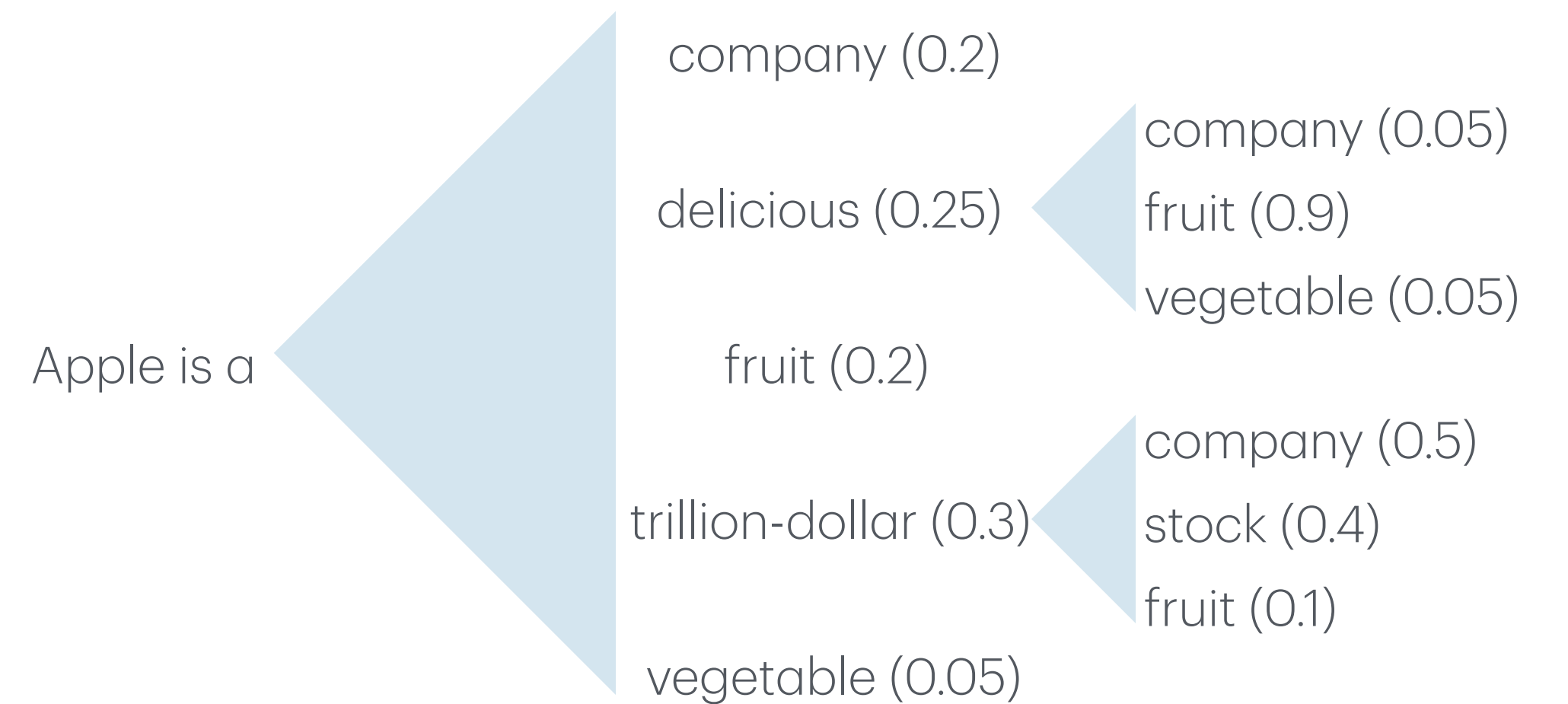
Sampling - Min-P

- Random sampling
 - Ignore $p < \alpha p_{\max}$
- 😊 Samples sound human-like
- 😊 Sampling fewer low-prob transitions
- Top-p better understood



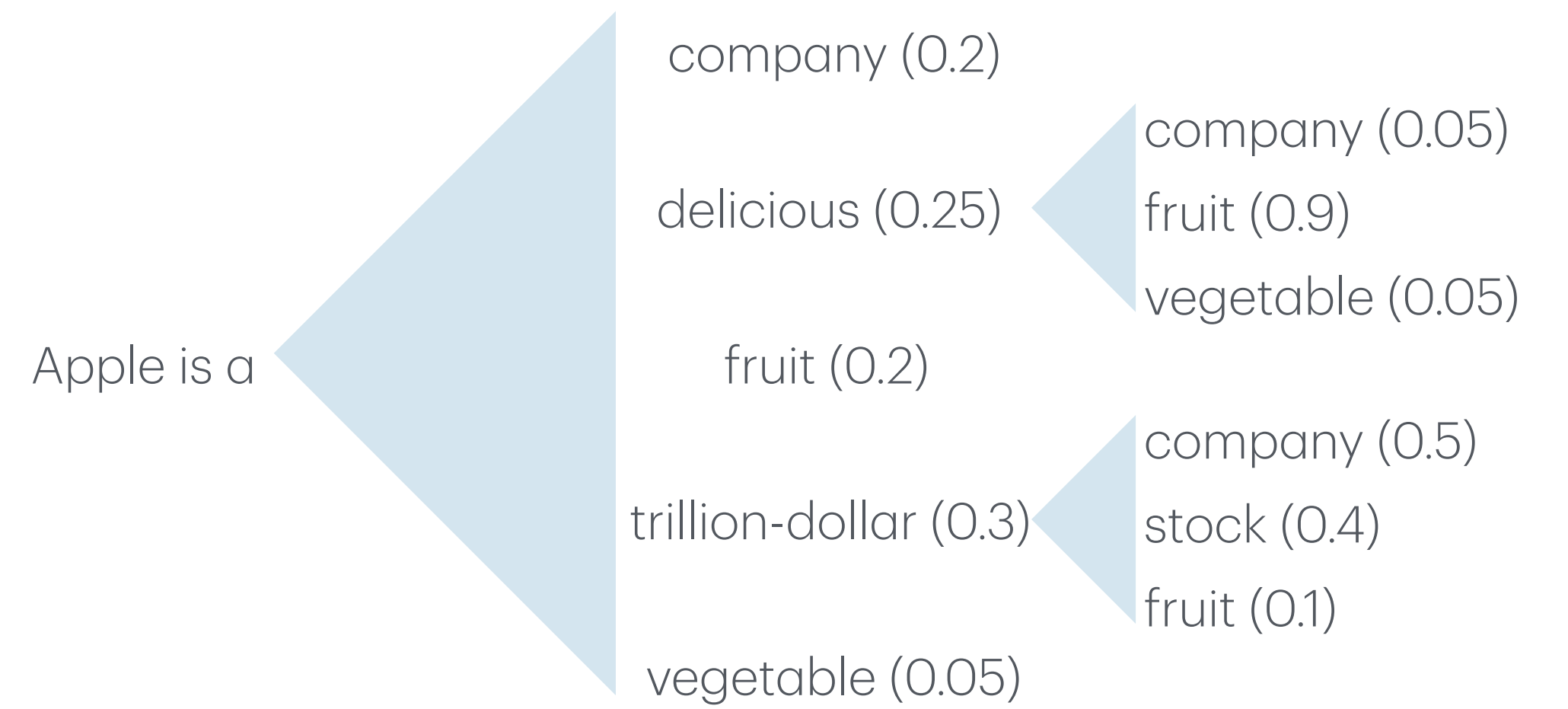
Sampling - Temperature

- More or less creative (random) writing by raising model prob to power $\frac{1}{T}$
- Temperature T
- Equivalent to multiplying logits with $\frac{1}{T}$
- $T = 0$: Greedy sampling
- $T \rightarrow \infty$: Uniform generation



Sampling - When do we stop?

- LLMs have special tokens [bos], [eos]



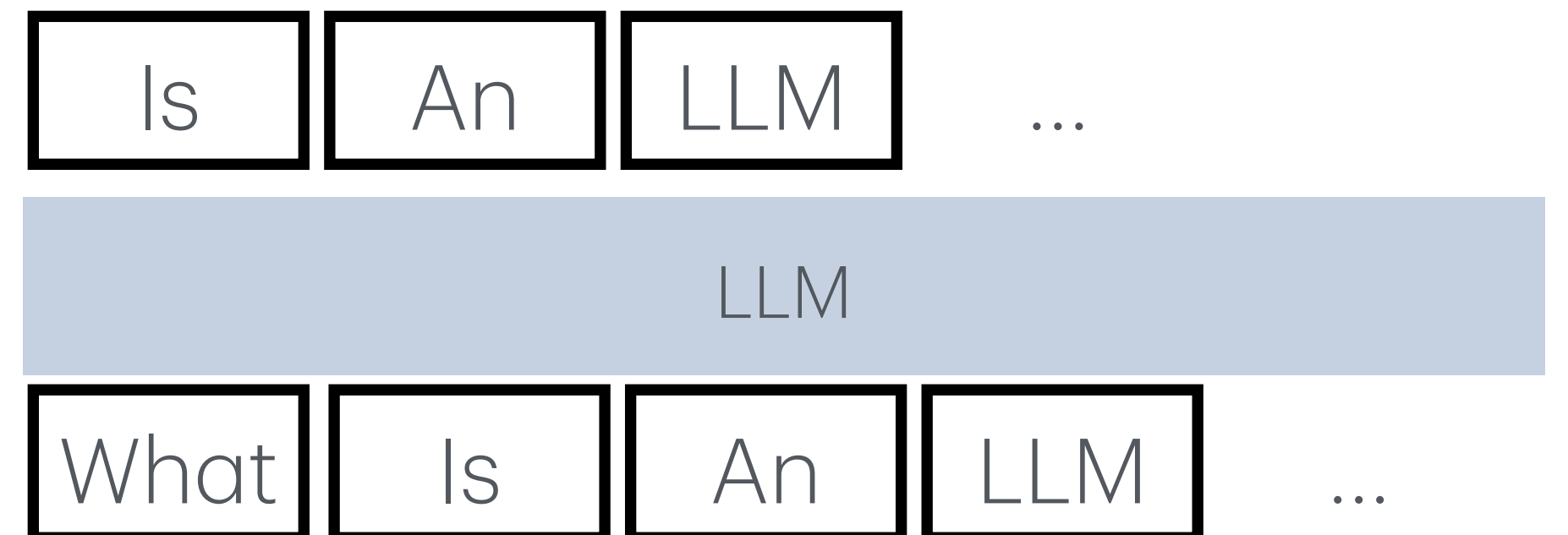
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- Generation / Sampling: $\mathbf{t} \sim P$

Distributions / logits



Embeddings
Output



References

- [1] Improving Language Understanding by Generative Pre-Training. Radford et al. 2018.
- [2] The Curious Case of Neural Text Degeneration. Holtzman et al. 2019.
- [3] Turning Up the Heat: Min-p Sampling for Creative and Coherent LLM Outputs. Nguyen et al. 2024.