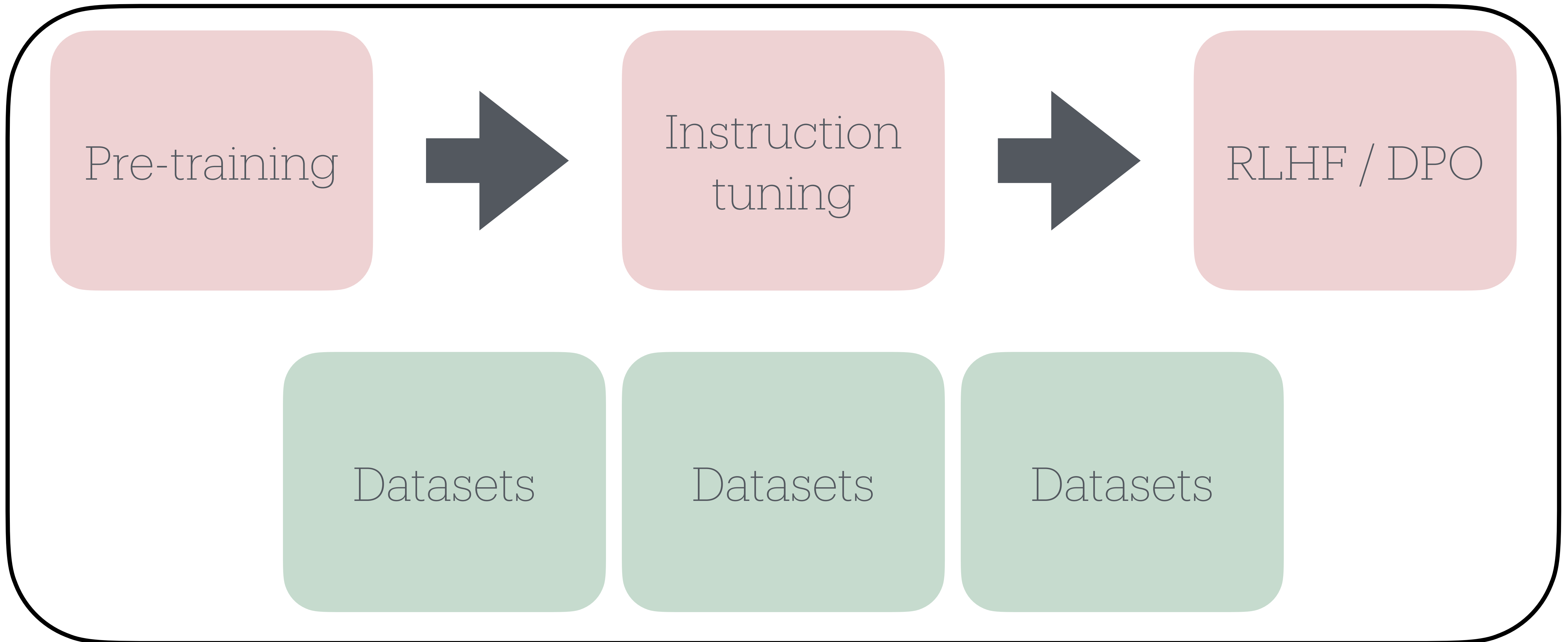


# Long Context

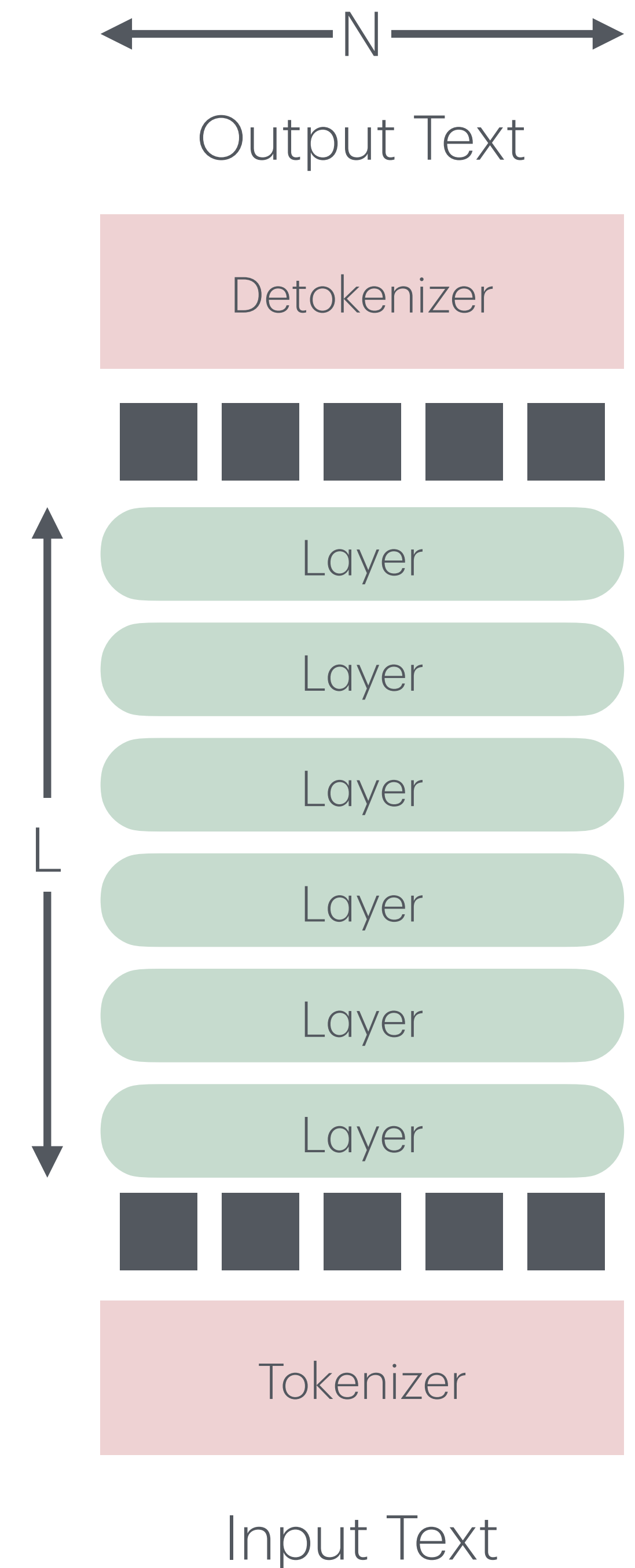
# Full Picture

Basic LLM



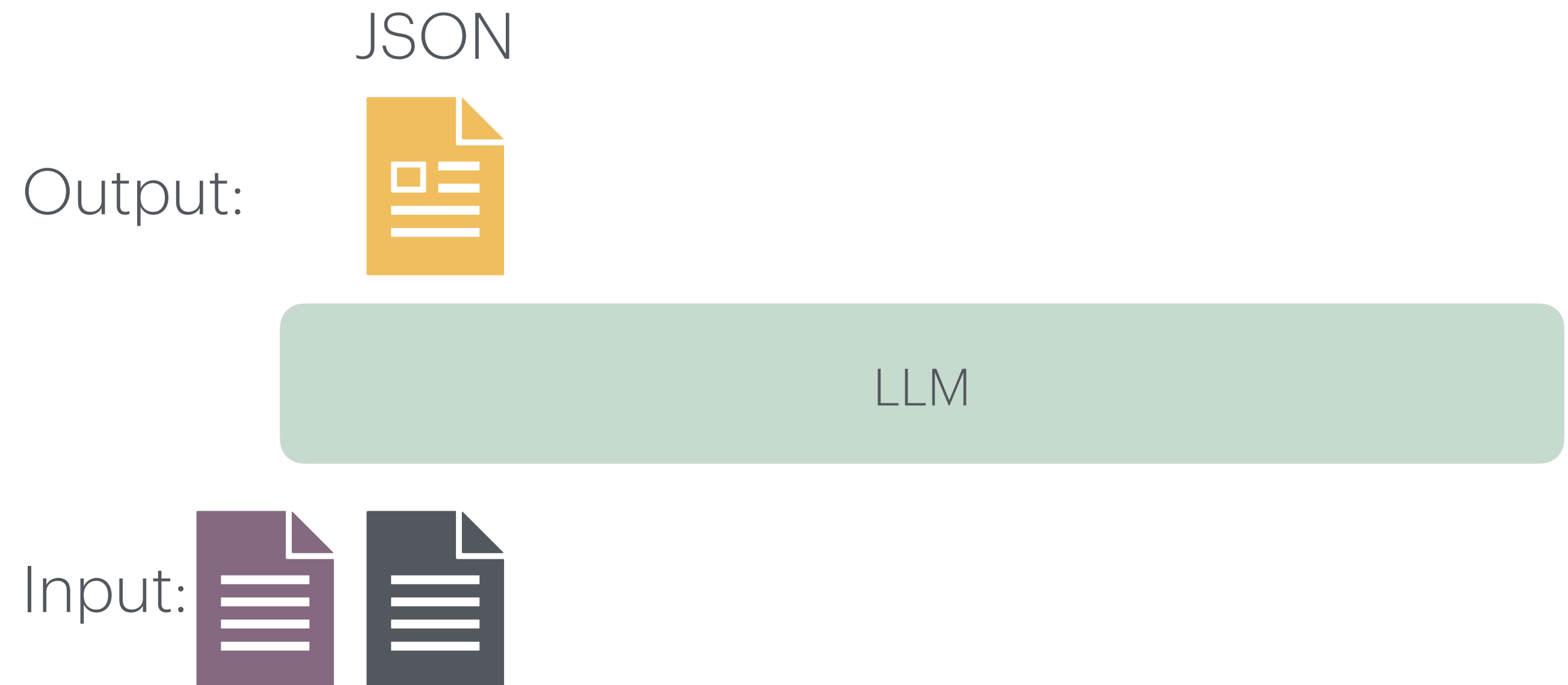
# Training and Generation

	Training	Training - Checkpointi	Generation	Paged Attention	Speculative decoding
Peak Memory	$O(NL)$	$O(NL^{1/2})$	$O(N)$	$O(NL)$	$O(NL)$
Runtime	$O(N^2L)$	$O(2 N^2L)$	$O(N^3L)$	$O(N^2L)$	$O(N^2L)$
# forward	1	1	N	N	$N / \alpha$



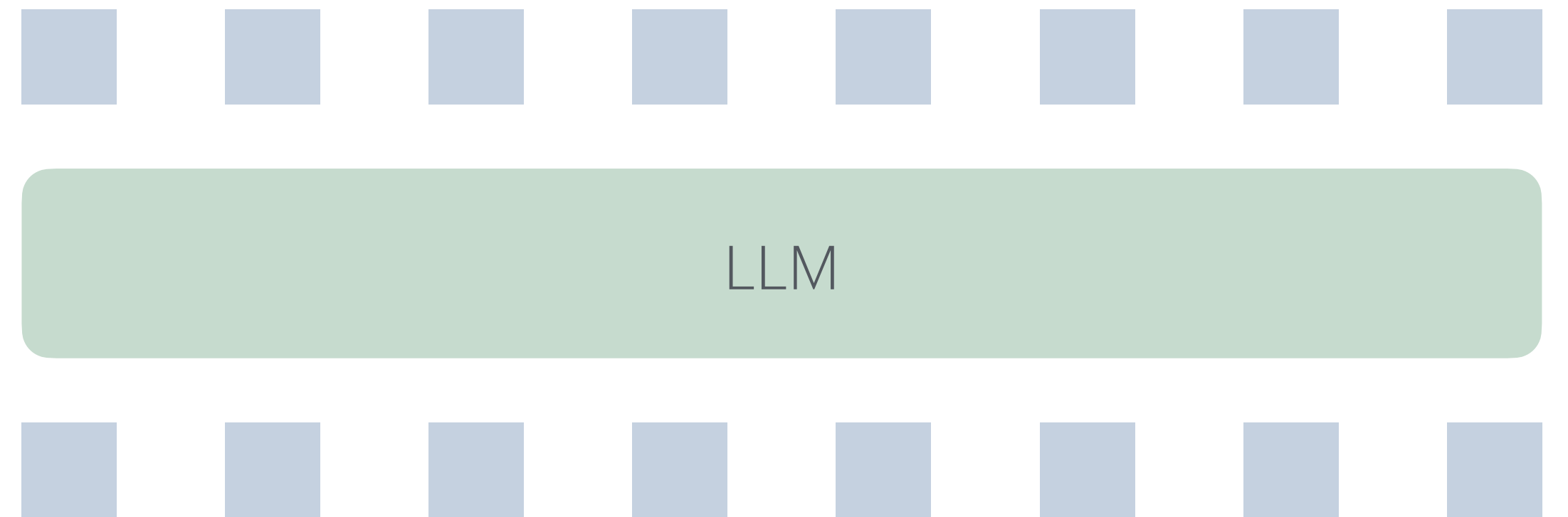
# Tools and Structured outputs

- Tools
  - Special tags, Special chat-template
- Structured output
  - Option 1.1: Write a robust parser (in python)
    - Let LLM know that you failed to parse
  - Option 1.2: Constrain output
  - Option 2: Use a tool, arguments = json fields



# Long Context

- Current models are **pre-trained** on **2-8k** token sequences



# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

???



Read these documents and find references to efficient long-context LLMs



# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

1. OOM (Out Of Memory)

???



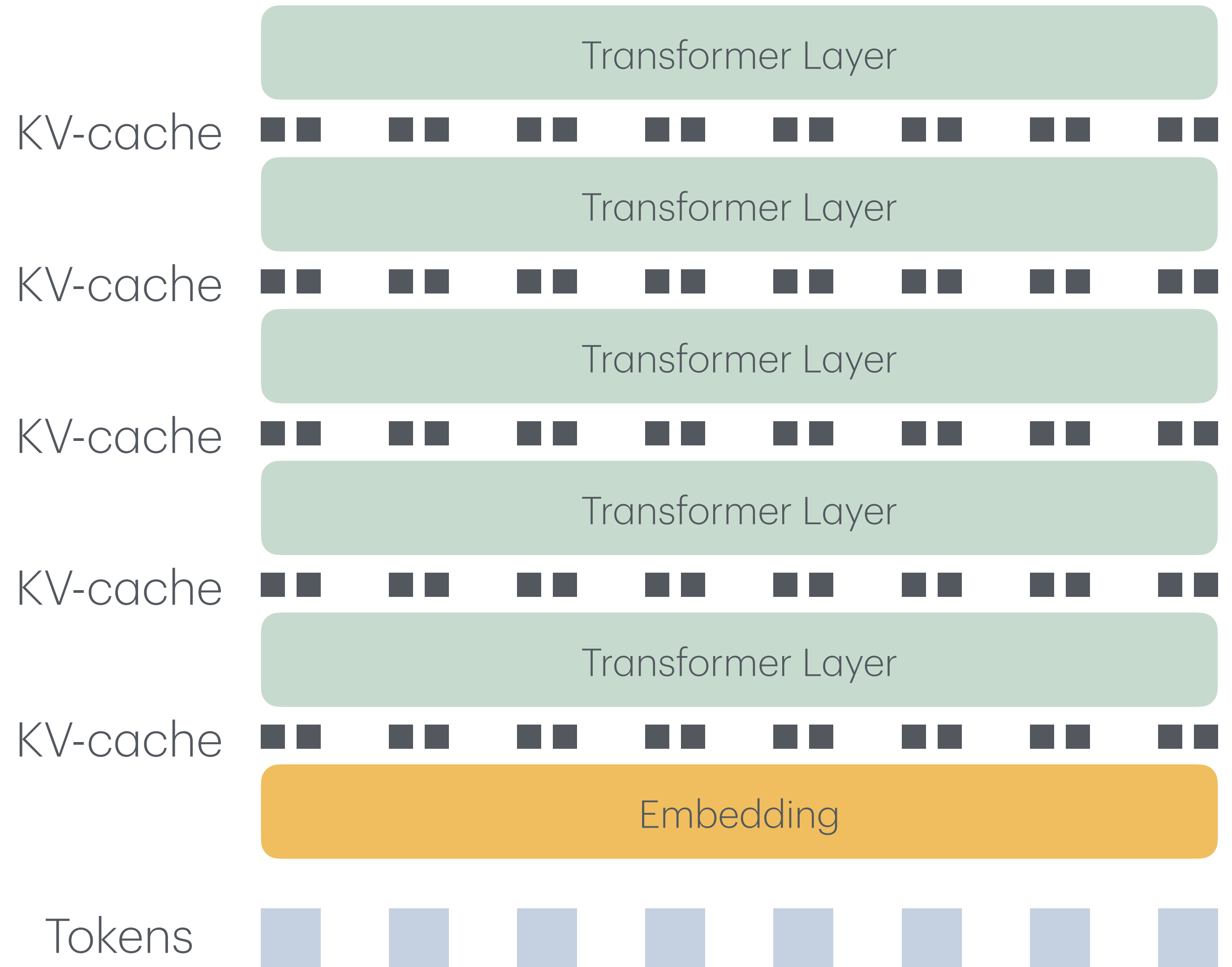
Read these documents and find references to efficient long-context LLMs



# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

1. OOM (Out Of Memory)





# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

1. OOM (Out Of Memory)
2. Model will be very slow

???

LLM

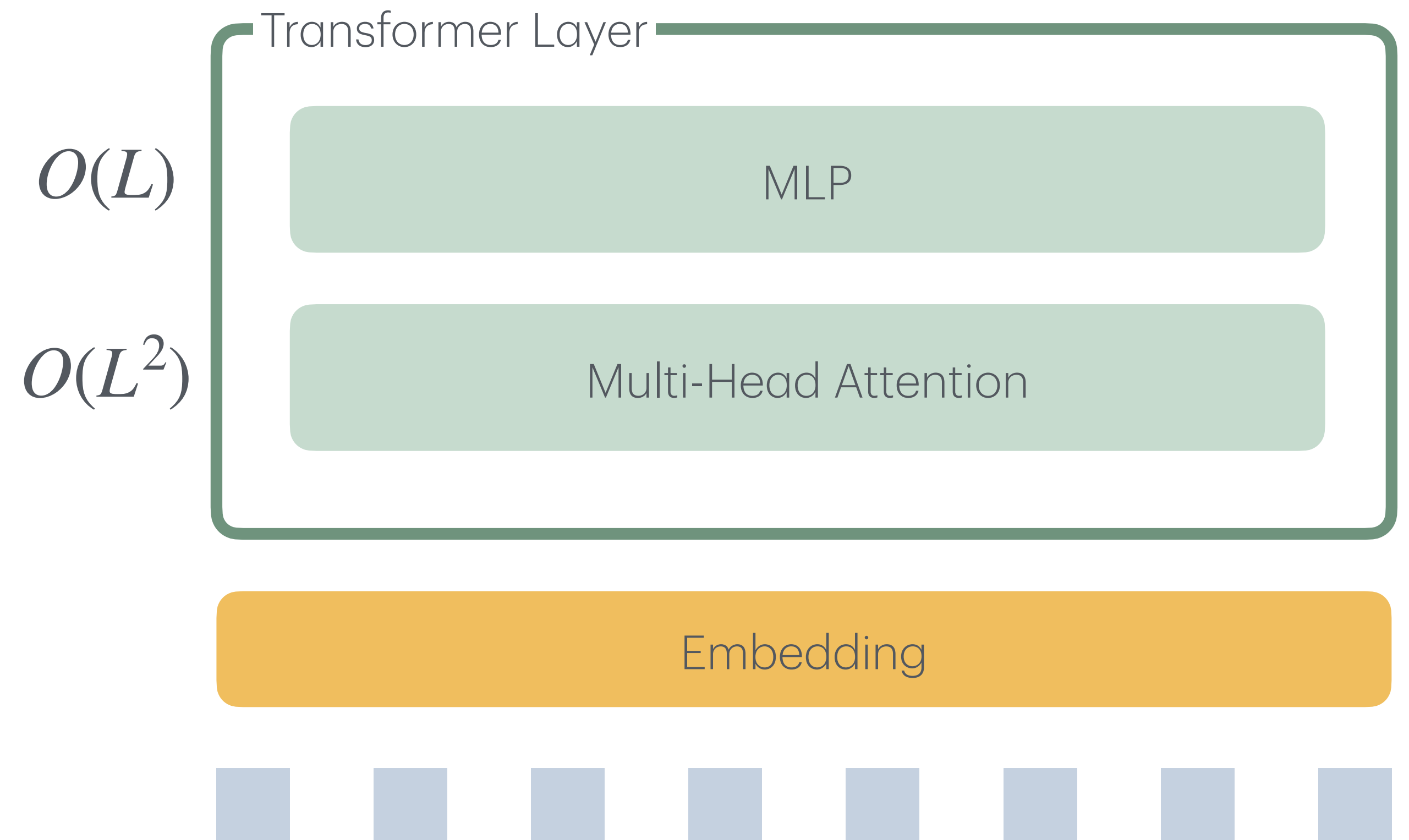
Read these documents and find references to efficient long-context LLMs



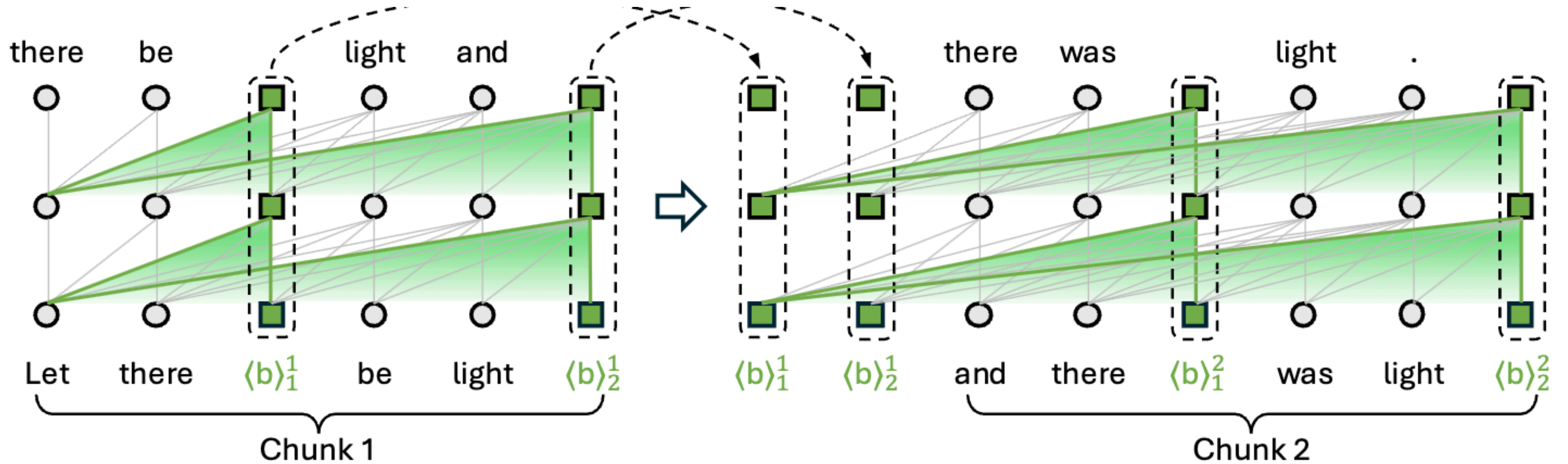
# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

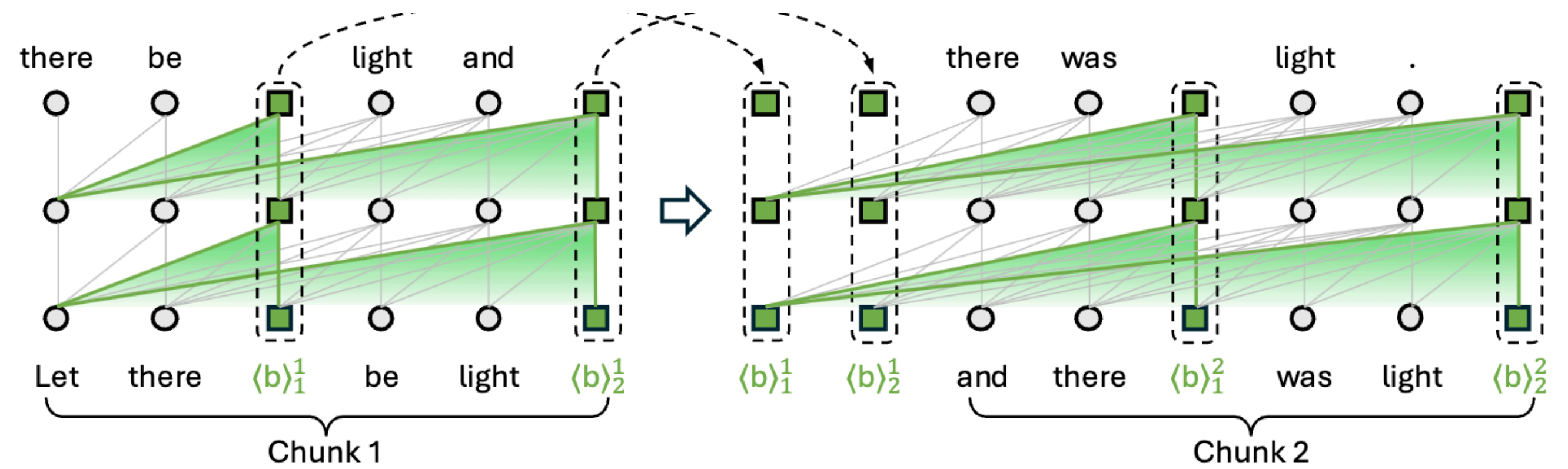
1. OOM (Out Of Memory)
2. Model will be very slow



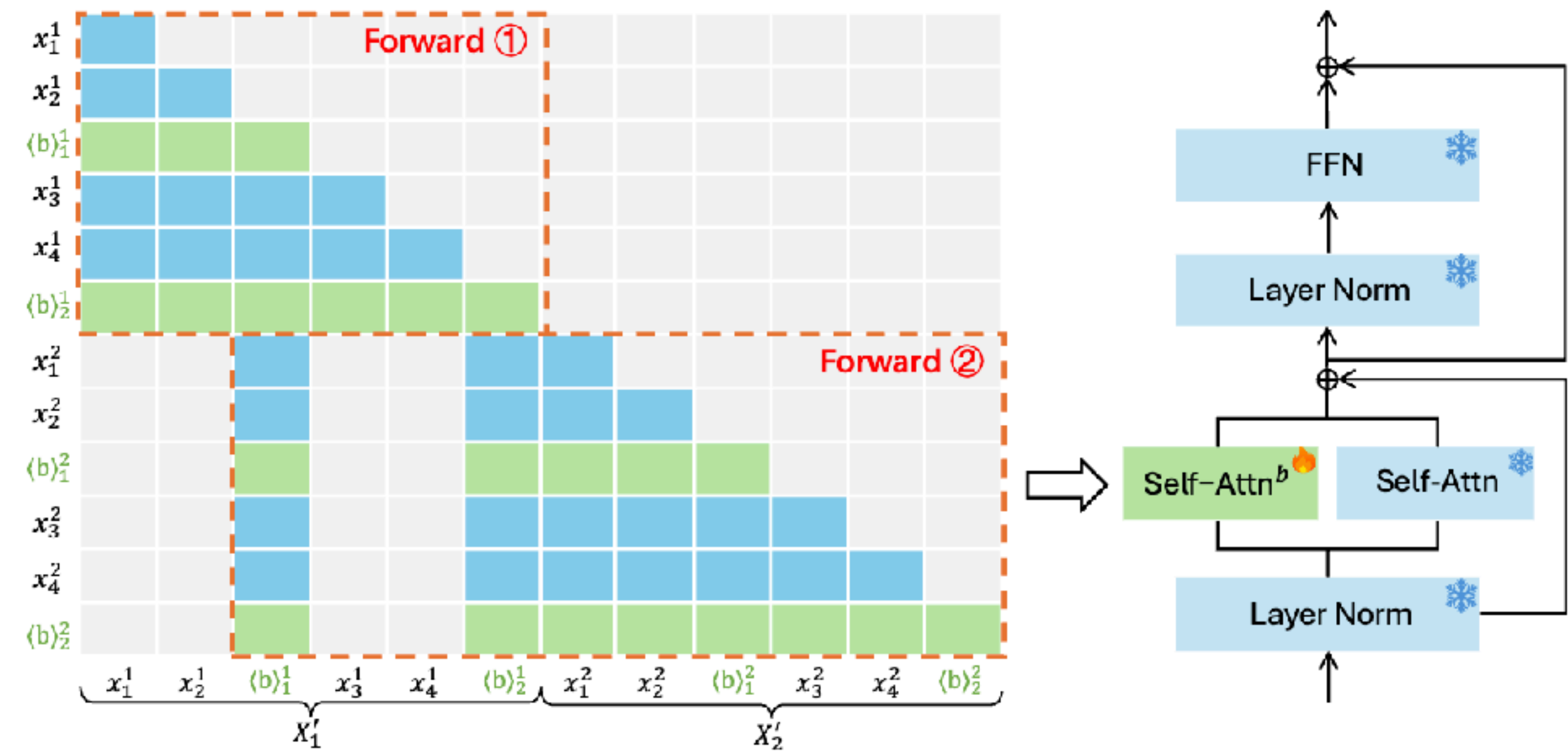
# Activation Beacon



# Activation Beacon



- Start from pre-trained model
- Partition sequence into chunks of 1024
- Pick  $k$  "beacons" per chunk
- Chunk  $n$  only sees beacons of chunks  $1 \dots n-1$
- Fine-tune



# Long Context

???

What happens if we feed ten's of thousands of tokens into an LLM?

1. ~~OOM (Out Of Memory)~~
2. ~~Model will be very slow~~

Activation  
Beacons  
and  
friends

Read these  
documents  
and find  
references to  
efficient  
long-context  
LLMs



LLM

# Long Context

???

What happens if we feed ten's of thousands of tokens into an LLM?

- ~~1. OOM (Out Of Memory)~~
  - ~~2. Model will be very slow~~
  3. Model will produce garbage outputs
- Activation Beacons and friends

Read these documents and find references to efficient long-context LLMs



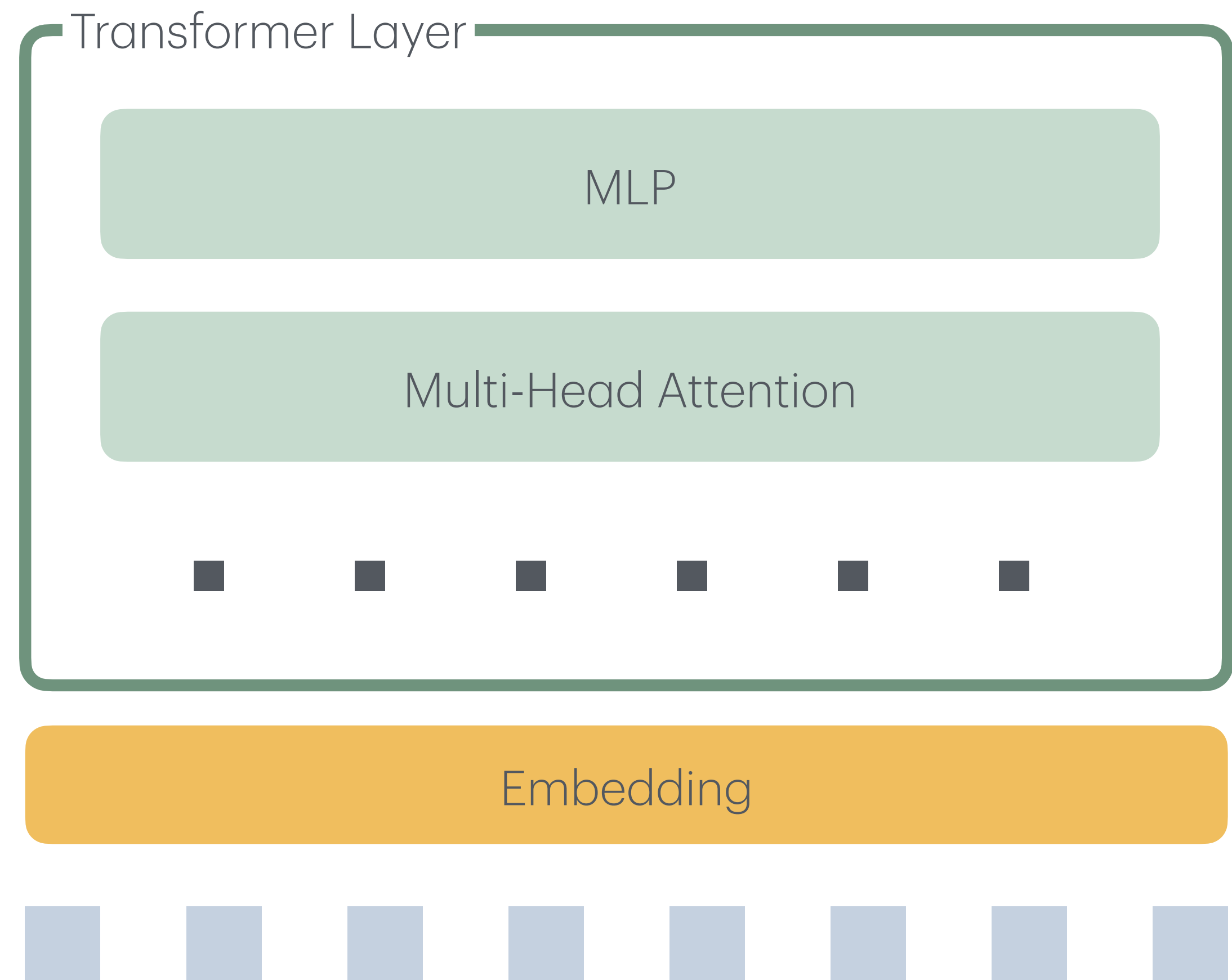
LLM

# Long Context

What happens if we feed ten's of thousands of tokens into an LLM?

1. ~~OOM (Out Of Memory)~~      Activation Beacons and friends
2. ~~Model will be very slow~~
3. Model will produce garbage outputs

Positional embedding



# Positional Embedding

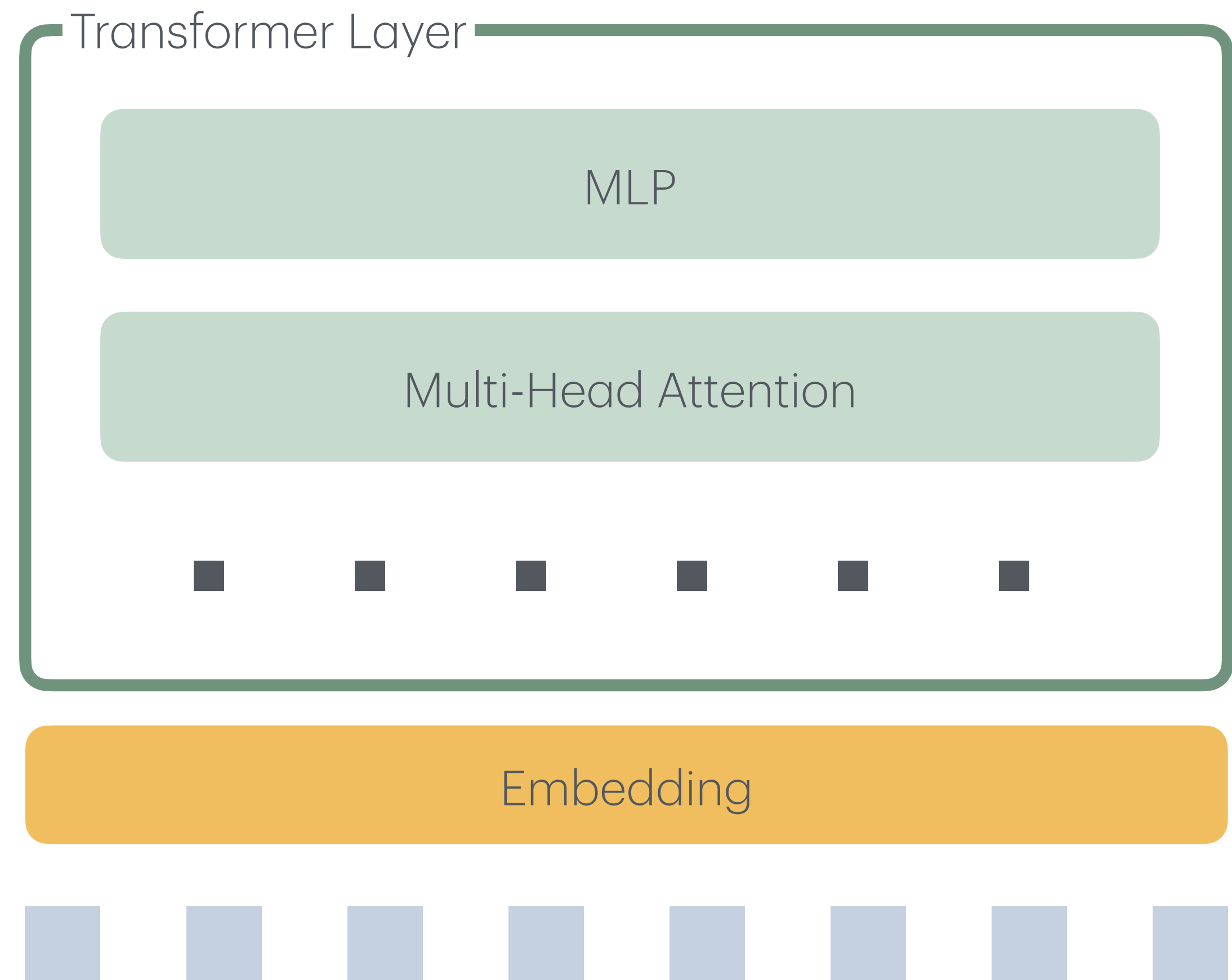
- Rotary Embeddings

$$f_{\{q,k\}}(\mathbf{x}_m, m) = \mathbf{R}_{\Theta, m}^d \mathbf{W}_{\{q,k\}} \mathbf{x}_m$$

$$\mathbf{R}_{\Theta, m}^d = \begin{pmatrix} \cos m\theta_1 & -\sin m\theta_1 & 0 & 0 & \cdots & 0 & 0 \\ \sin m\theta_1 & \cos m\theta_1 & 0 & 0 & \cdots & 0 & 0 \\ 0 & 0 & \cos m\theta_2 & -\sin m\theta_2 & \cdots & 0 & 0 \\ 0 & 0 & \sin m\theta_2 & \cos m\theta_2 & \cdots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \cdots & \cos m\theta_{d/2} & -\sin m\theta_{d/2} \\ 0 & 0 & 0 & 0 & \cdots & \sin m\theta_{d/2} & \cos m\theta_{d/2} \end{pmatrix}$$

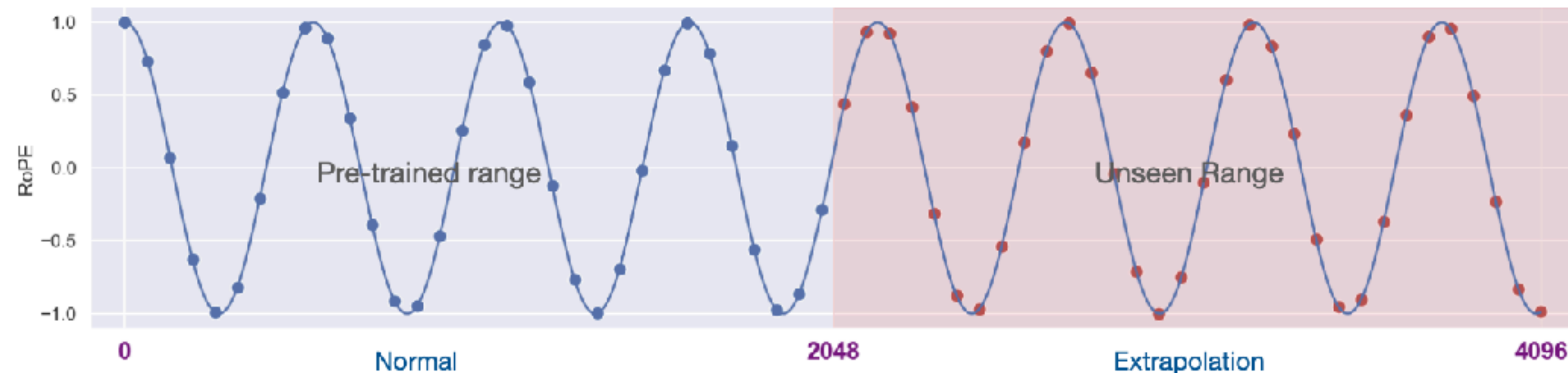
$$\mathbf{q}_m^\top \mathbf{k}_n = (\mathbf{R}_{\Theta, m}^d \mathbf{W}_q \mathbf{x}_m)^\top (\mathbf{R}_{\Theta, n}^d \mathbf{W}_k \mathbf{x}_n) = \mathbf{x}^\top \mathbf{W}_q \mathbf{R}_{\Theta, n-m}^d \mathbf{W}_k \mathbf{x}_n$$

Positional embedding





# Positional Embedding



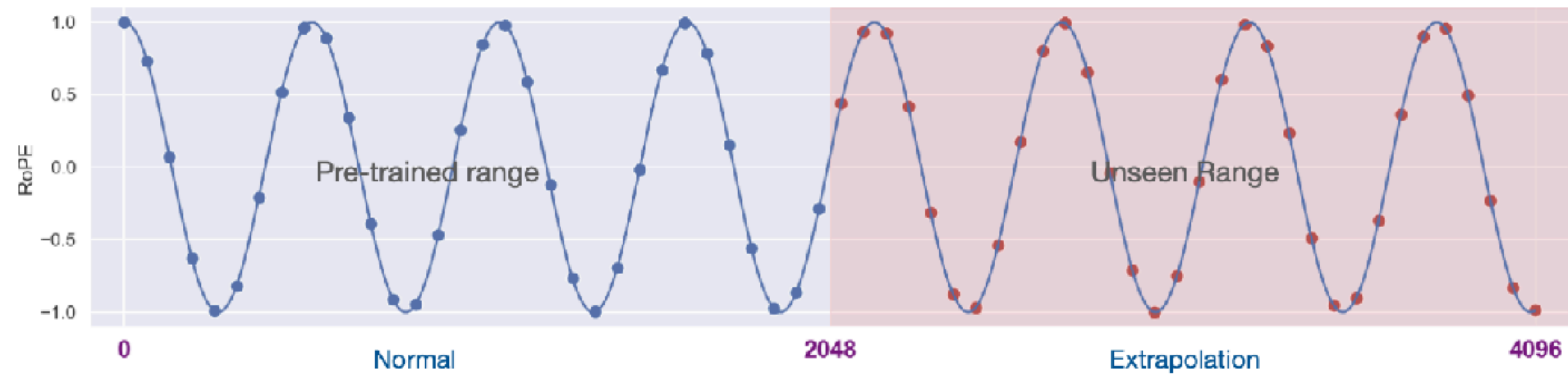
- Rotary Embeddings
- Fixed context length during training
  - Longer context for inference

$$f_{\{q,k\}}(\mathbf{x}_m; m) = \mathbf{R}_{\Theta, m}^d \mathbf{W}_{\{q,k\}} \mathbf{x}_m$$

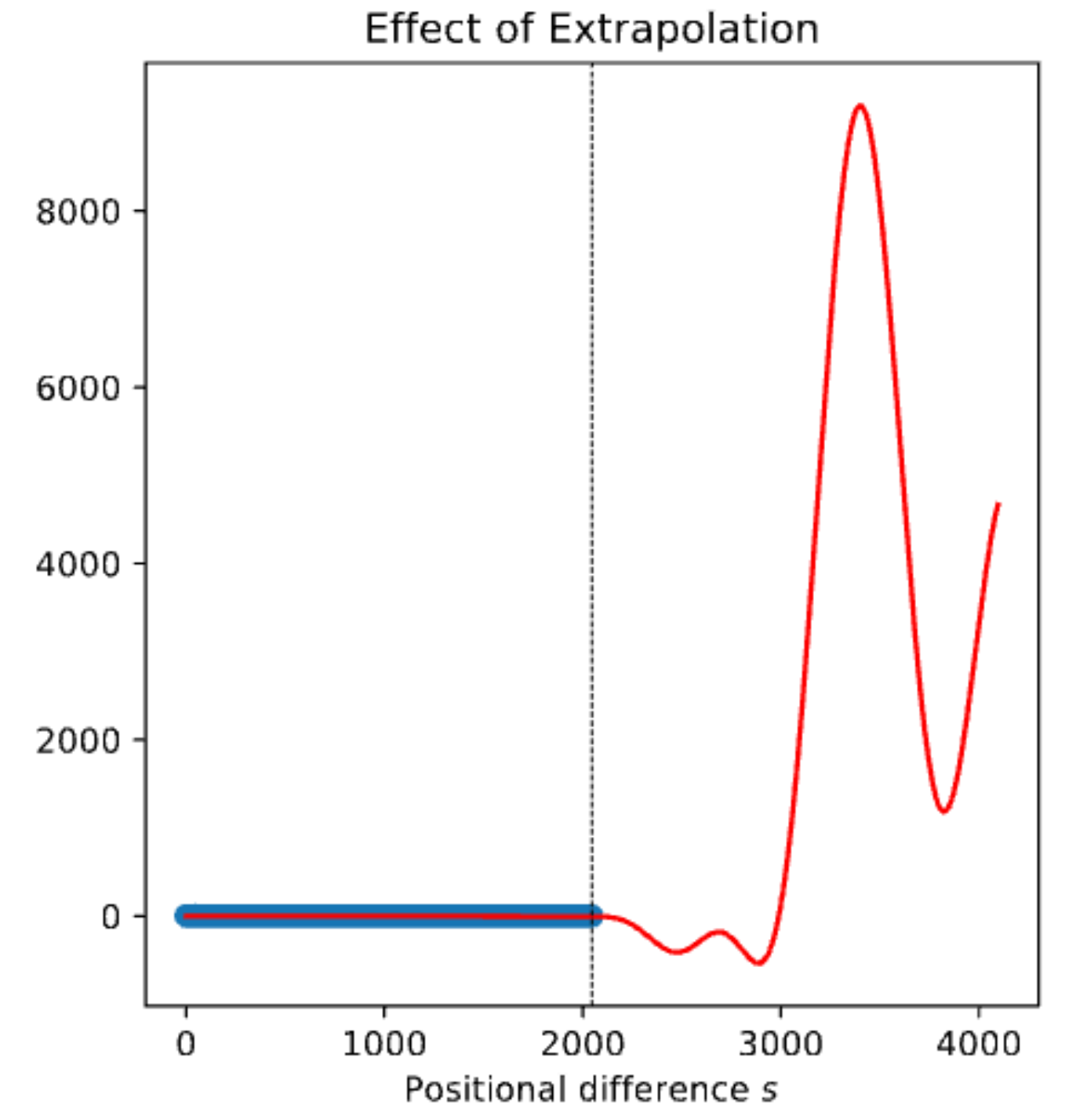
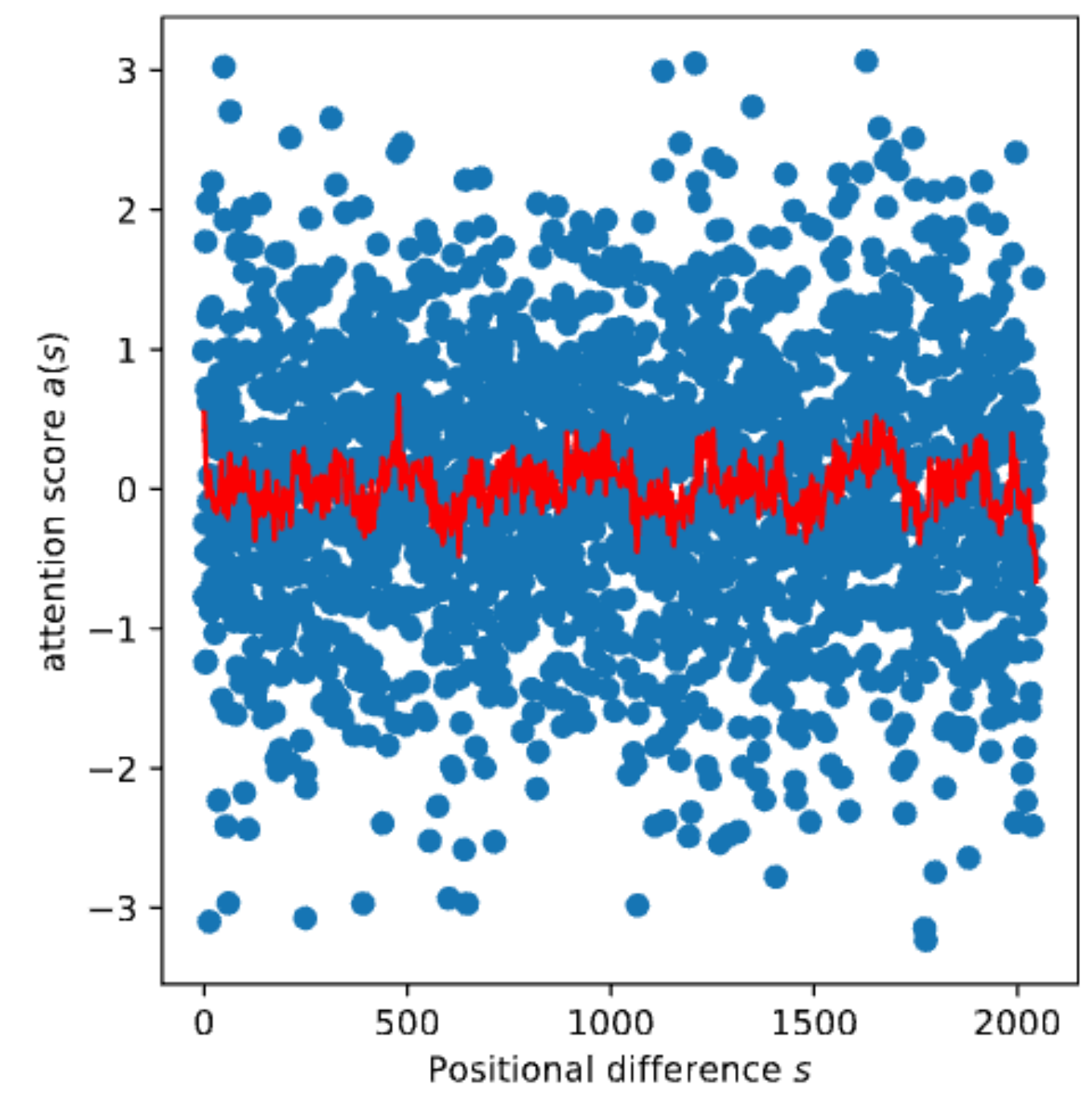
$$\mathbf{R}_{\Theta, m}^d = \begin{pmatrix} \cos m\theta_1 & -\sin m\theta_1 & 0 & 0 & \dots & 0 & 0 \\ \sin m\theta_1 & \cos m\theta_1 & 0 & 0 & \dots & 0 & 0 \\ 0 & 0 & \cos m\theta_2 & -\sin m\theta_2 & \dots & 0 & 0 \\ 0 & 0 & \sin m\theta_2 & \cos m\theta_2 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \dots & \cos m\theta_{d/2} & -\sin m\theta_{d/2} \\ 0 & 0 & 0 & 0 & \dots & \sin m\theta_{d/2} & \cos m\theta_{d/2} \end{pmatrix}$$

$$\mathbf{q}_m^\top \mathbf{k}_n = (\mathbf{R}_{\Theta, m}^d \mathbf{W}_q \mathbf{x}_m)^\top (\mathbf{R}_{\Theta, n}^d \mathbf{W}_k \mathbf{x}_n) = \mathbf{x}^\top \mathbf{W}_q \mathbf{R}_{\Theta, n-m}^d \mathbf{W}_k \mathbf{x}_n$$

# Positional Embedding



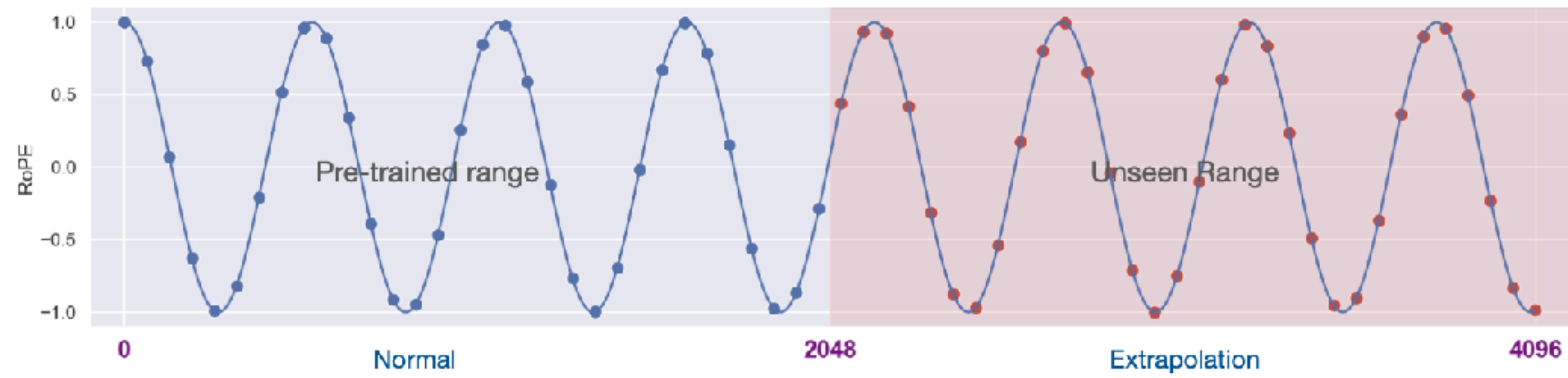
- Rotary Embeddings
  - Do not extrapolate well



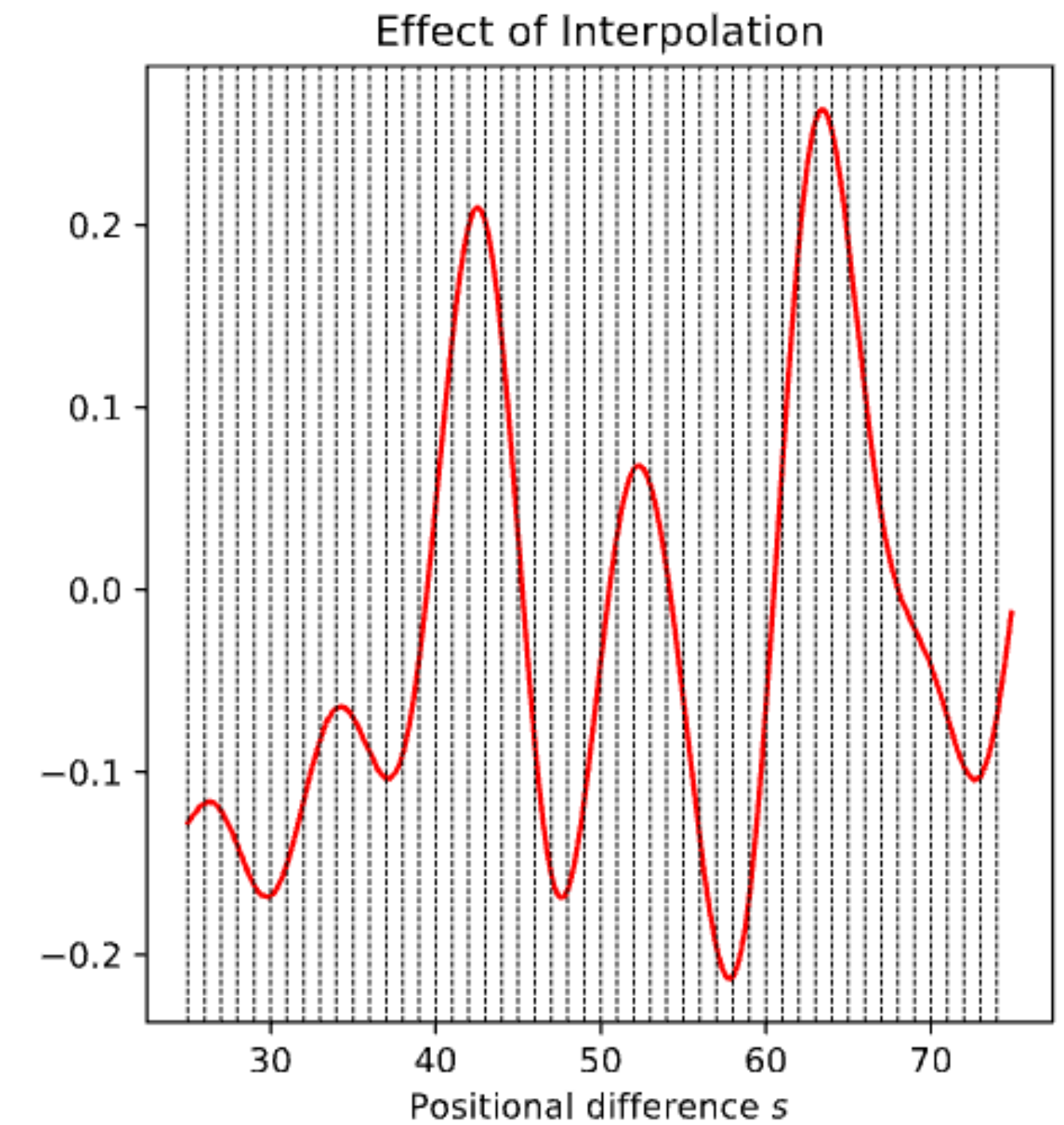
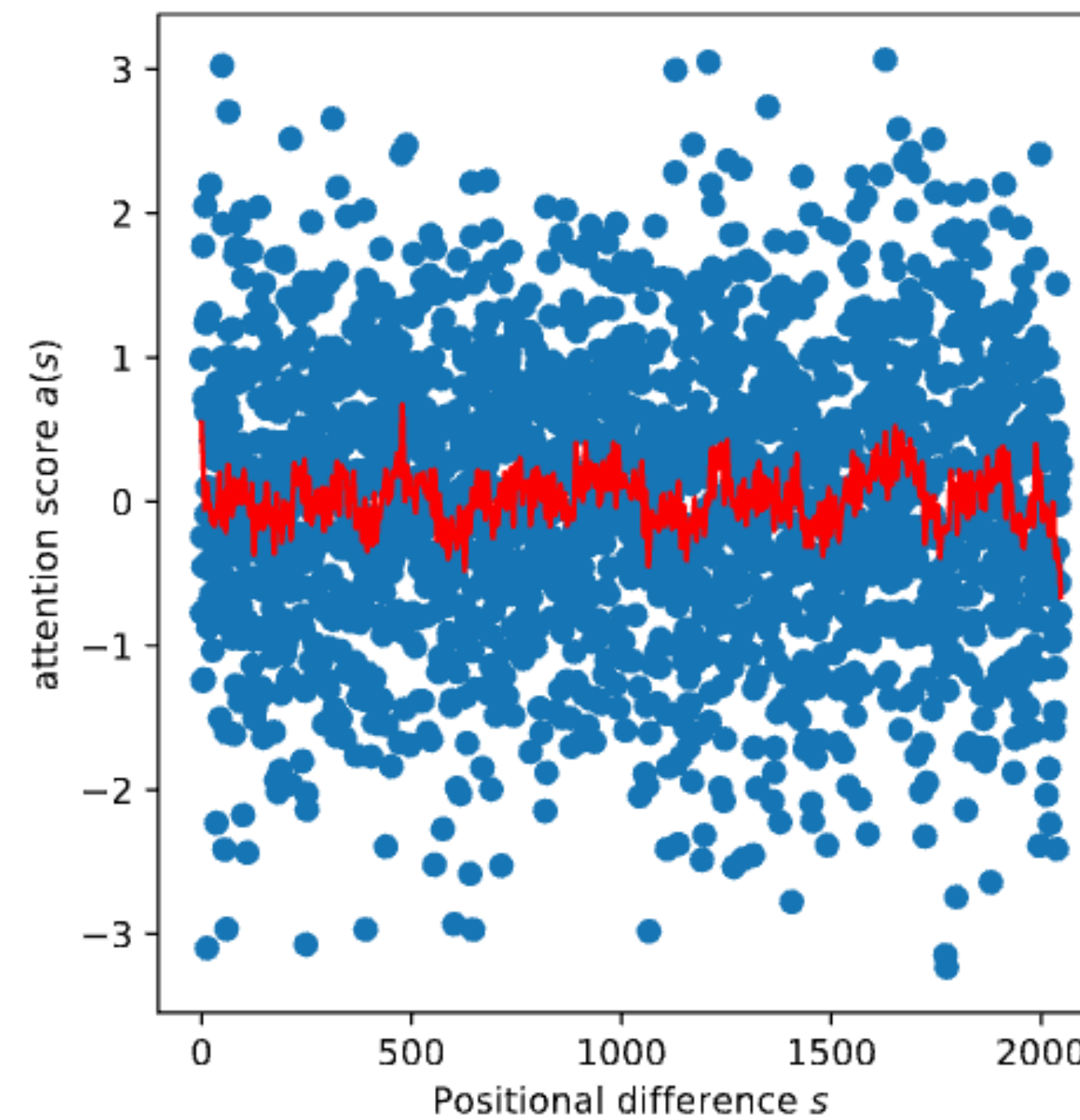
RoFormer: Enhanced Transformer with Rotary Position Embedding, Su et al 2021

Extending Context Window of Large Language Models via Positional Interpolation, Chen et al 2023

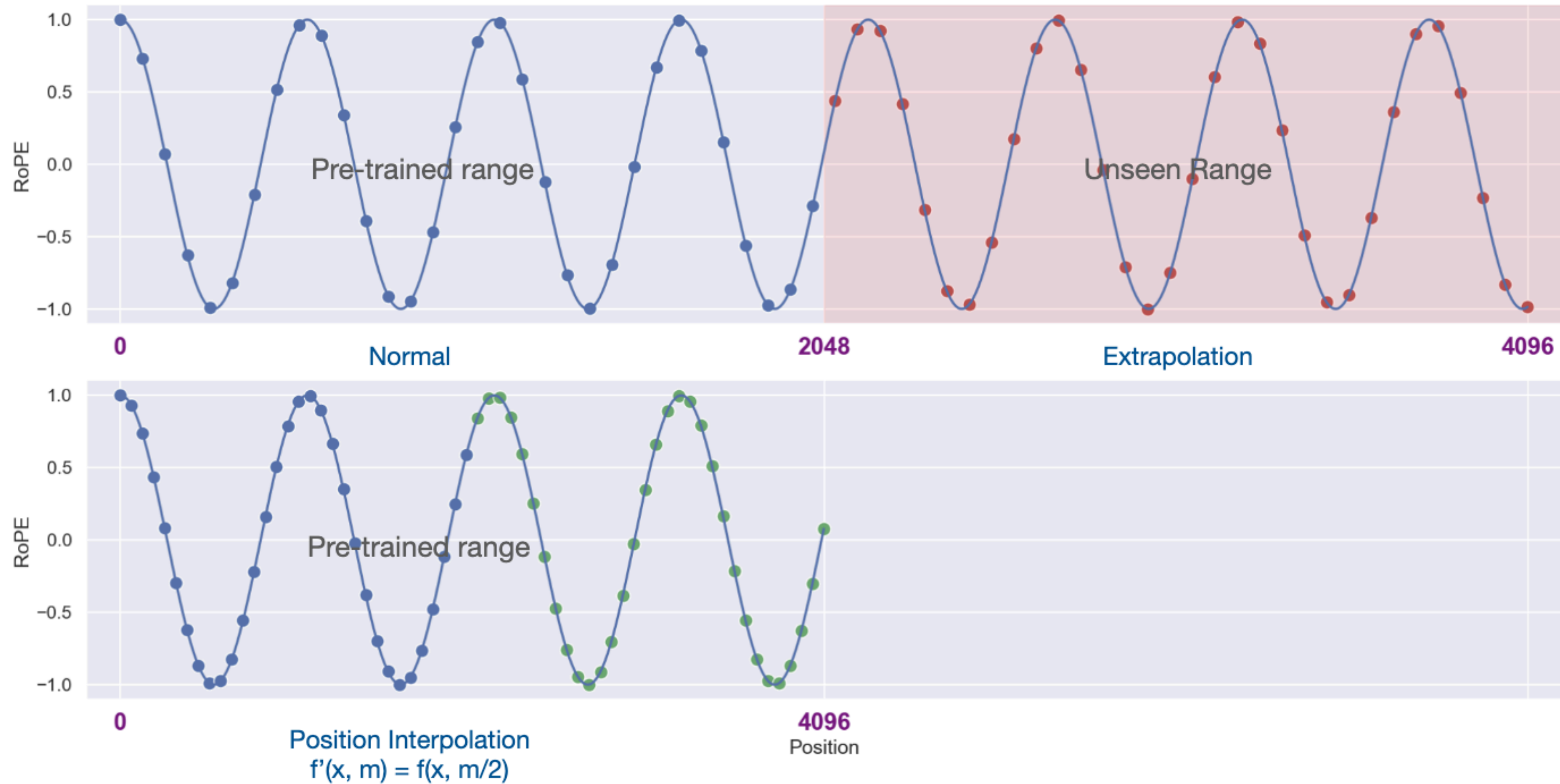
# Positional Embedding



- Rotary Embeddings
  - Do not extrapolate well
  - But they interpolate



# RoPE Scaling

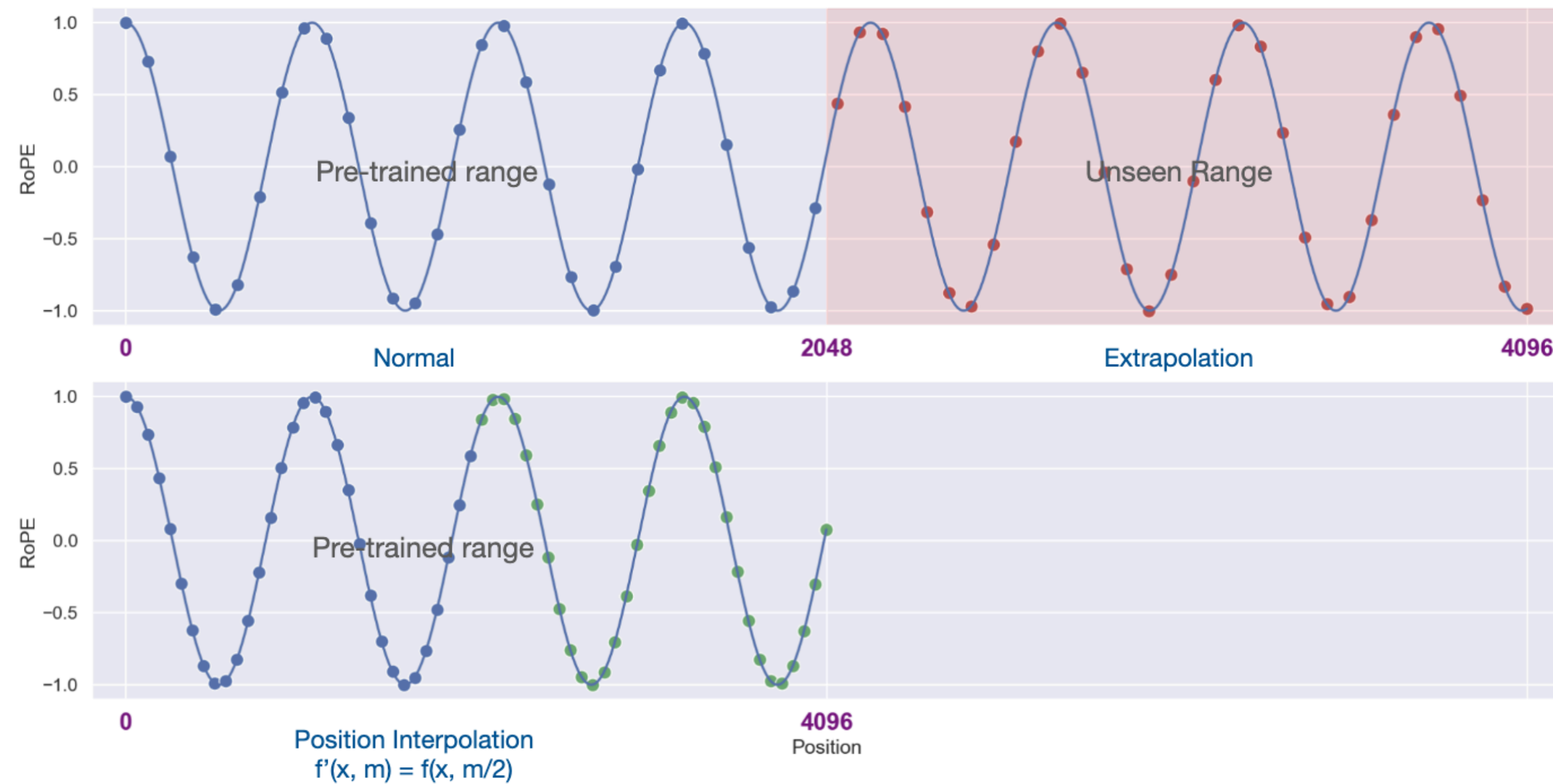


RoFormer: Enhanced Transformer with Rotary Position Embedding, Su et al 2021

Extending Context Window of Large Language Models via Positional Interpolation, Chen et al 2023

# RoPE Scaling

- Extrapolation
  - Make token stream **longer**
  - Does not generalize
- RoPE Scaling
  - Make token stream **denser**
  - Model generalizes
- Widely used



RoFormer: Enhanced Transformer with Rotary Position Embedding, Su et al 2021

Extending Context Window of Large Language Models via Positional Interpolation, Chen et al 2023

# Long Context

???

What happens if we feed ten's of thousands of tokens into an LLM?

- ~~1. OOM (Out Of Memory)~~
- ~~2. Model will be very slow~~
- ~~3. Model will produce garbage outputs~~

RoPE scaling

Activation  
Beacons  
and  
friends

Read these documents and find references to efficient long-context LLMs



LLM

# Long Context

- Current models are **pre-trained** on **2-8k** token sequences
- Late stage pre-training **8k-128k**
  - RoPE Scaling
- Fine-tuned on variable length sequences

???

LLM

Read these documents and find references to efficient long-context LLMs



# References

- [1] Long Context Compression with Activation Beacon, Zhang et al. 2024 ([link](#))
- [2] RoFormer: Enhanced Transformer with Rotary Position Embedding, Su et al 2021 ([link](#))
- [3] Extending Context Window of Large Language Models via Positional Interpolation, Chen et al 2023 ([link](#))