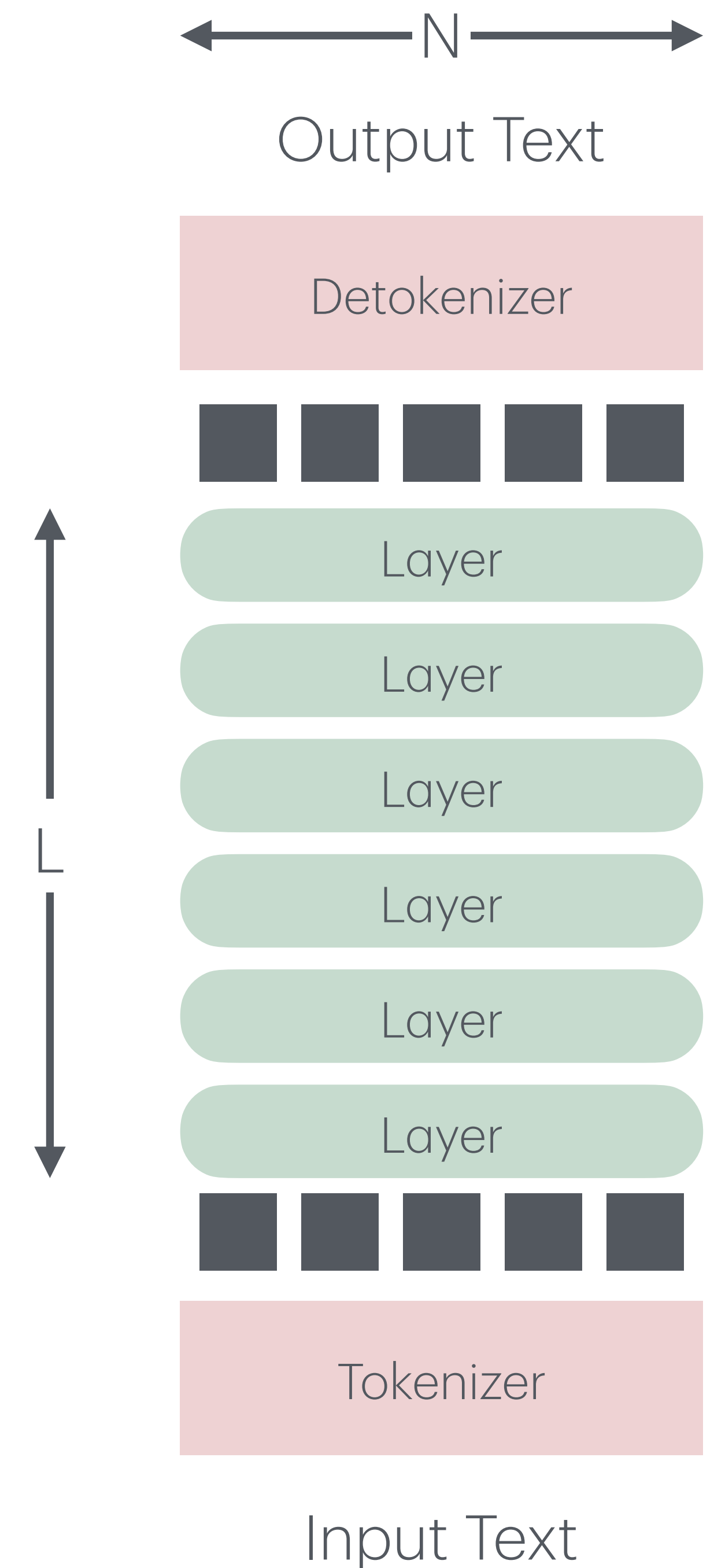


Page Attention

Training and Generation

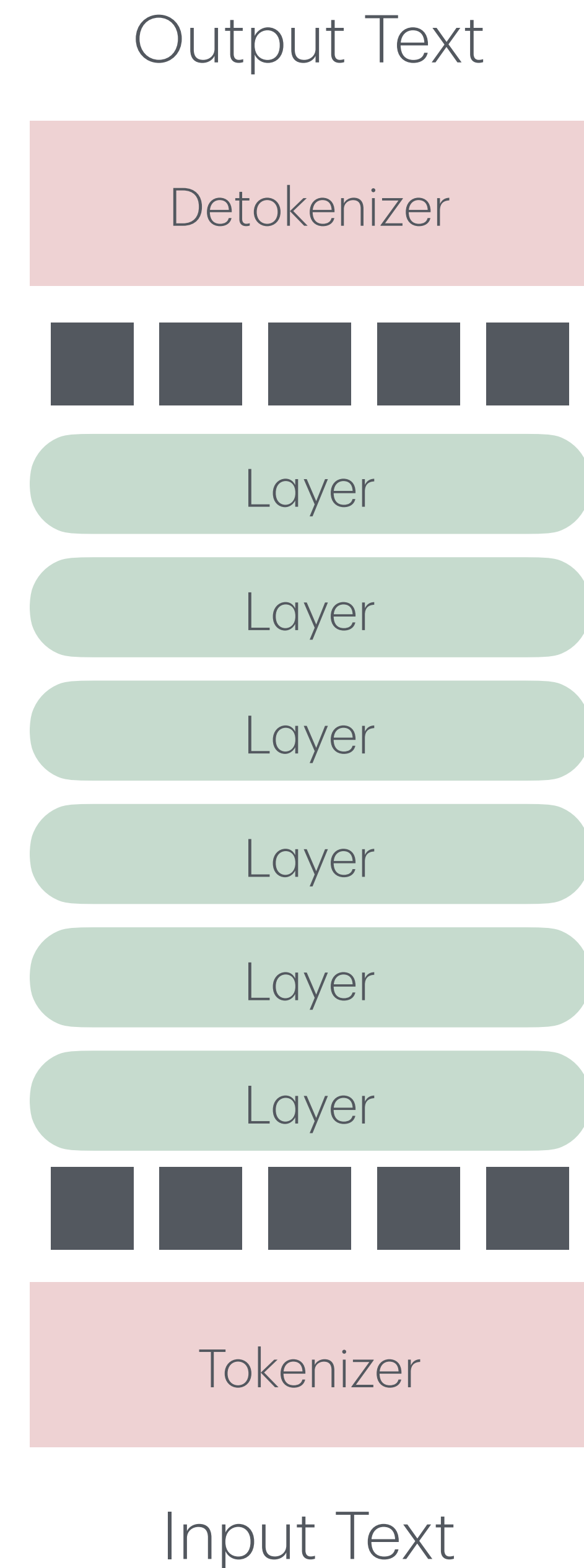
Vanilla Generation

	Training	Training - Checkpointing	Generation
Peak Memory	$O(NL)$	$O(NL^{1/2})$	$O(N)$
Runtime	$O(N^2L)$	$O(2 N^2L)$	$O(N^3L)$
# forward calls	1	1	N

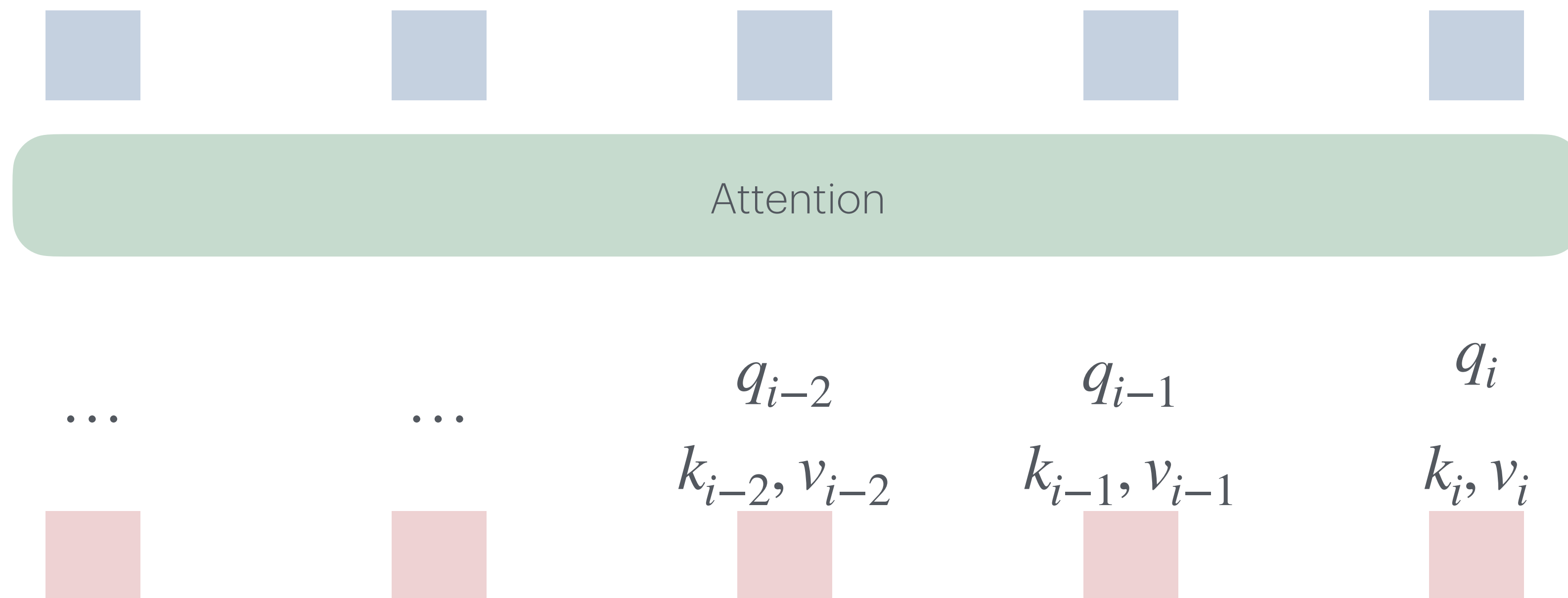


Generation

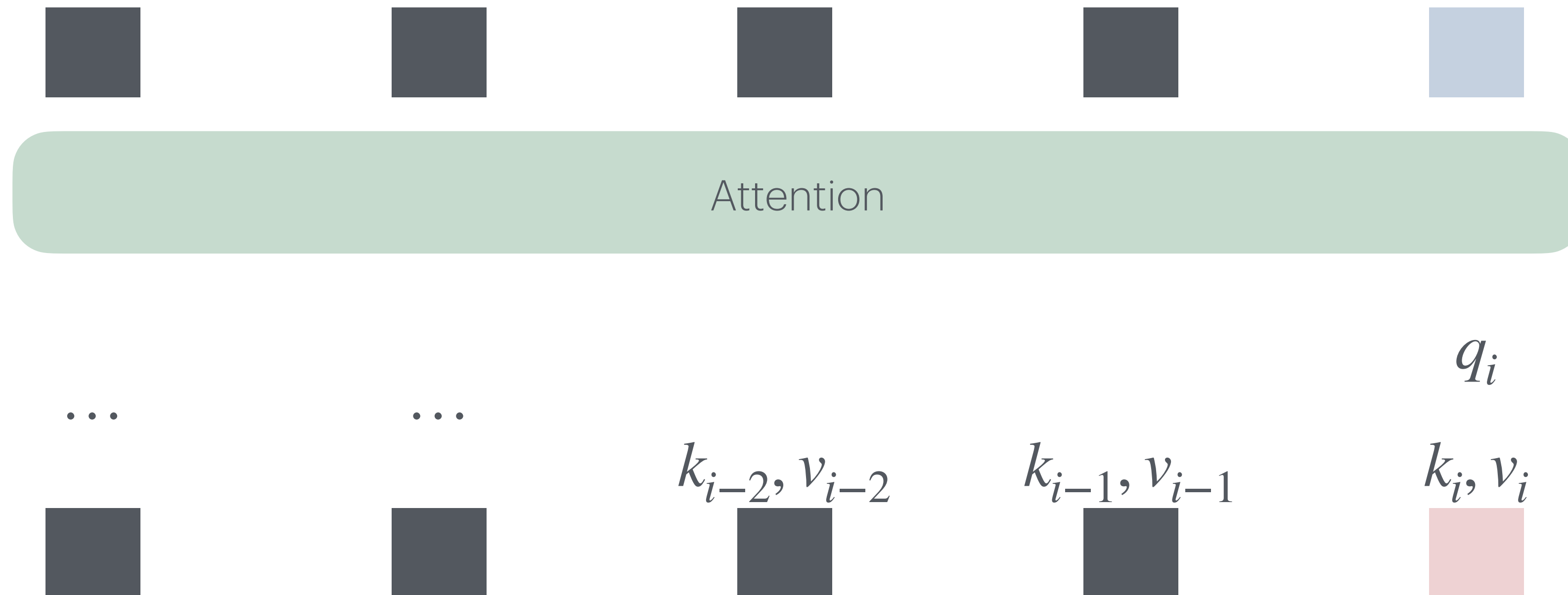
- Step 1: Tokenize
- Step 2: $N \times$ Forward
- Step 3: Detokenize



Vanilla Attention

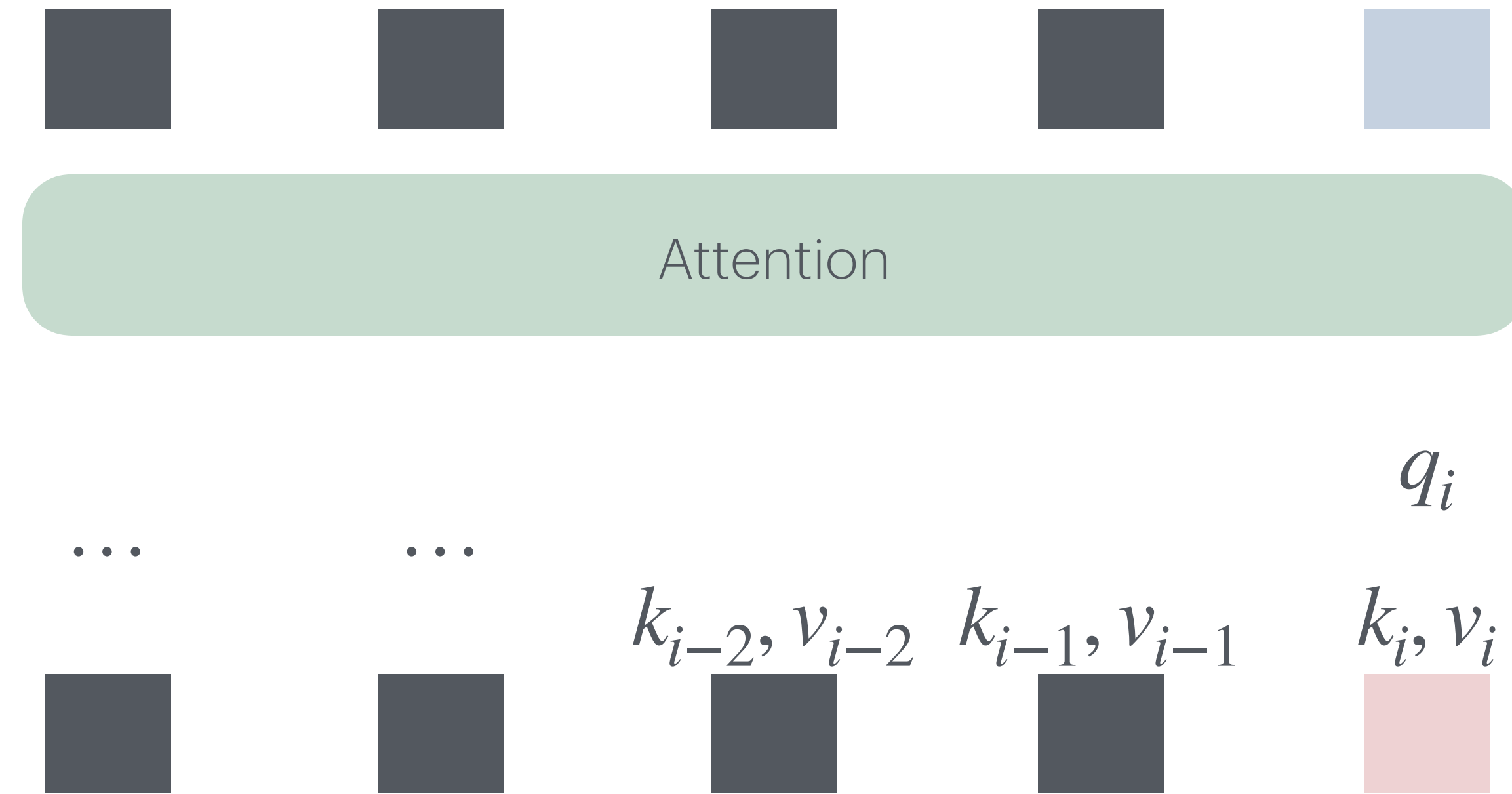


Paged Attention



Paged Attention - Analysis

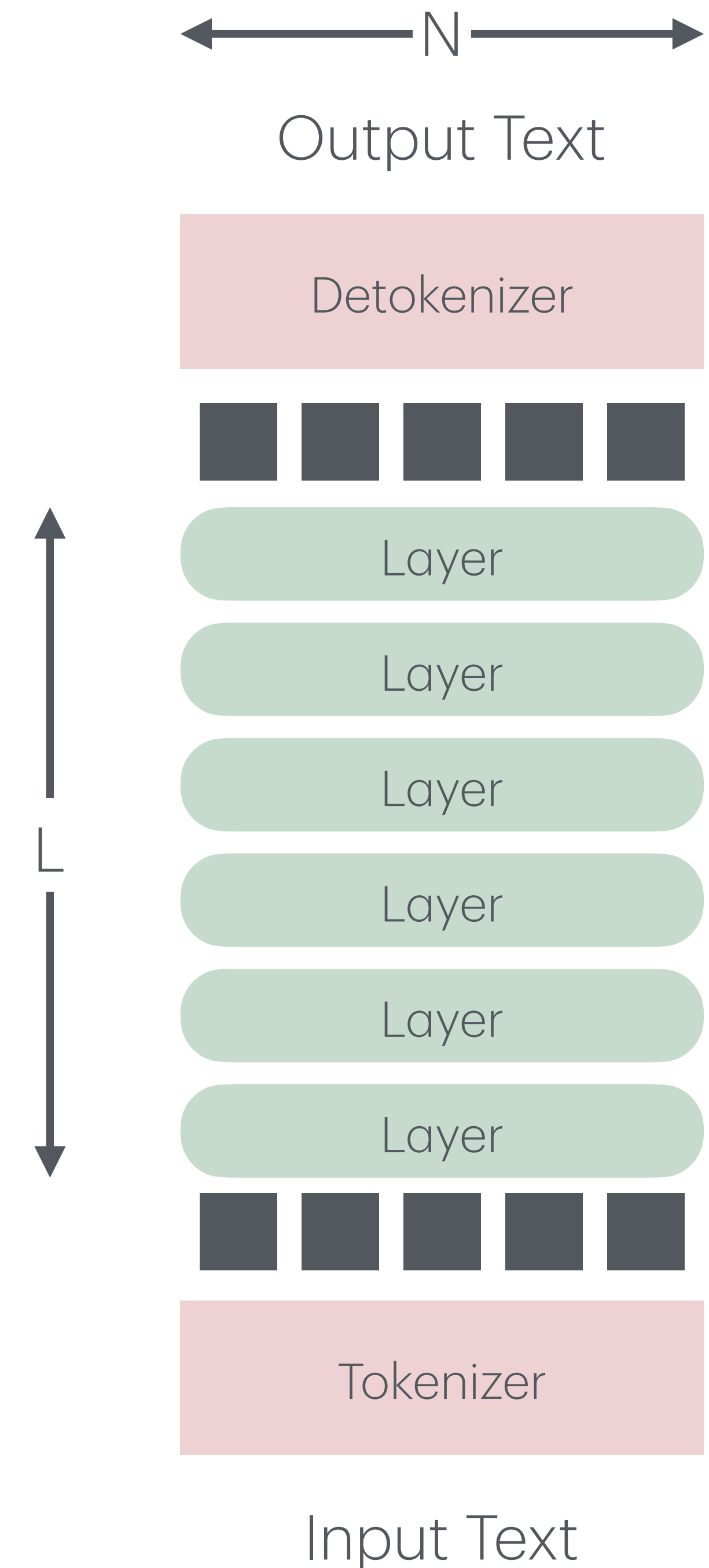
- Cache keys and value
 - $O(NL)$ memory
- Less computation
 - $O(NL)$ per output token



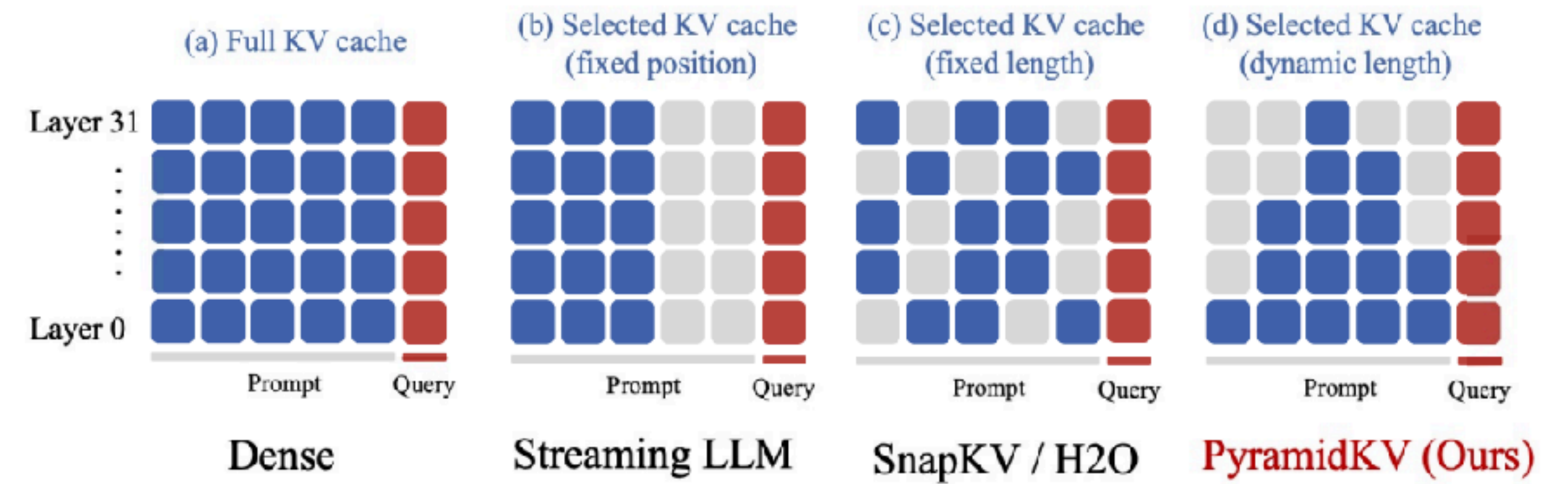
Training and Generation

Paged Attention

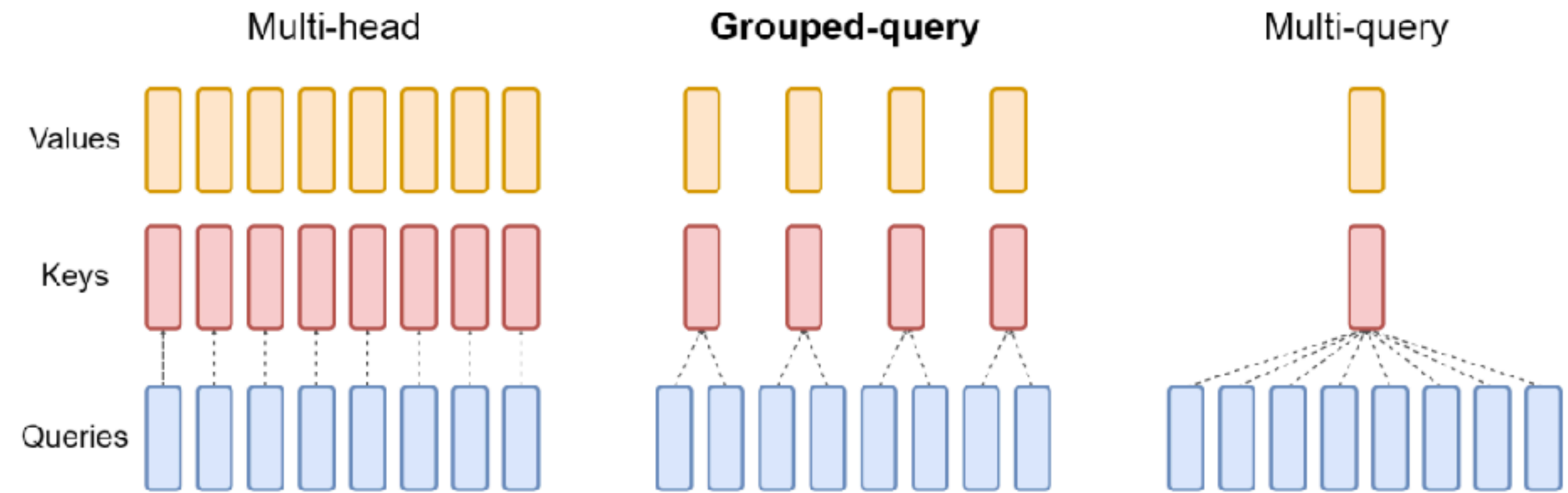
	Training	Training - Checkpointing	Generation	Paged Attention
Peak Memory	$O(NL)$	$O(NL^{1/2})$	$O(N)$	$O(NL)$
Runtime	$O(N^2L)$	$O(2 N^2L)$	$O(N^3L)$	$O(N^2L)$
# forward calls	1	1	N	N



Open Problem



- A more efficient KV-Cache
 - Group Query Attention
 - Pruning
 - Low-rank representations?
- Connection to state-space models



References

- [1] Efficient Memory Management for Large Language Model Serving with PagedAttention, Kwon et al 2023. ([link](#))
- [2] PyramidKV: Dynamic KV Cache Compression based on Pyramidal Information Funneling, Cai et al 2024. ([link](#))
- [3] GQA: Training Generalized Multi-Query Transformer Models from Multi-Head Checkpoints, Ainslie et al 2023. ([link](#))